

Two Examples of Integrated Optimization

Evolutionary Computing in Practice GECCO 2006

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Overview

- ▶ Engineering Optimization
 - ▶ Requirements
 - ▶ Industries
- ▶ What it means ...
- ▶ Requirements for a tool
- ▶ Examples
- ▶ Is it worth doing it ?

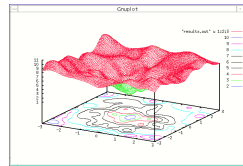
Engineering Optimization

General Aspects

Function

$$quality = \sum_{i=1}^{15} weight_i \cdot \left(\frac{calculated_i - desired_i}{scale_i} \right)^2$$

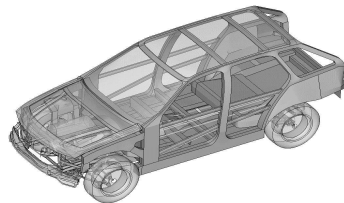
Model from Data



Subjective



Simulation



Experiment



Function(s)

$$f_i(\vec{y}) = \dots$$

Business Process Model

Evaluation

EA-Optimizer

Requirements I

- ▲ Very few function evaluations!
 - ▲ Simulator run times often many hours
- ▲ Tight business constraints on runtime
 - ▲ E.g., 2 weeks maximum (time pressure)
- ▲ Workflow support required
 - ▲ Coupling with simulators
 - ▲ Analysis of results
 - ▲ Great graphical user interface needed

Requirements II

- ▲ Optimizer requirements
 - ▲ Easy to use
 - ▲ $n > 100$, but number of evaluations often ~ 150
 - ▲ Many nonlinear constraints
 - ▲ Multiobjective needed
 - ▲ Robustness analysis needed
 - ▲ Mixed-integer needed
 - ▲ ...

Industries

- ▲ Automotive
- ▲ Aerospace
- ▲ Chemistry
- ▲ Engines, Turbines
- ▲ ...



HONDA



CORNING
Discovering Beyond Imagination

SIEMENS

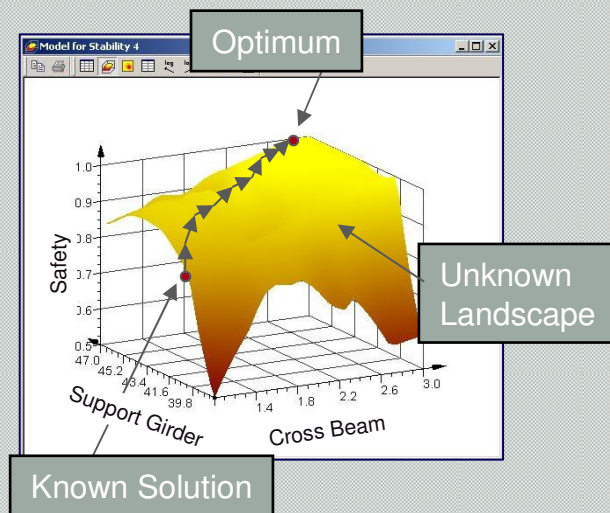
A Solution for ...

Intelligent
Computing

Intelligent
Computing

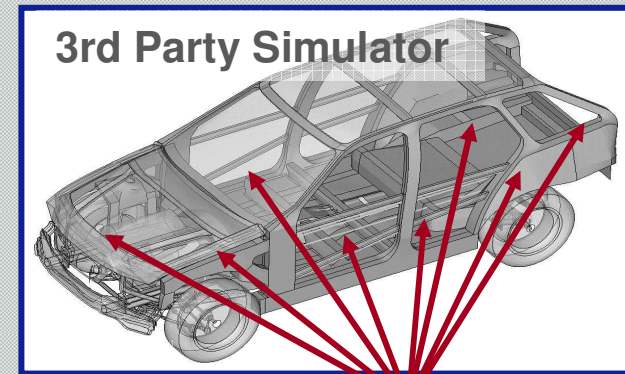
(Expensive) Computer
Experiments

A Challenging Example: Car Body Design



Global
Optimization

Finite Element
Mesh of 130,000;
Runtime: ~ 1 day



Thickness
of 109 Units

Two Must-Haves ...

... to accomplish such complex tasks:

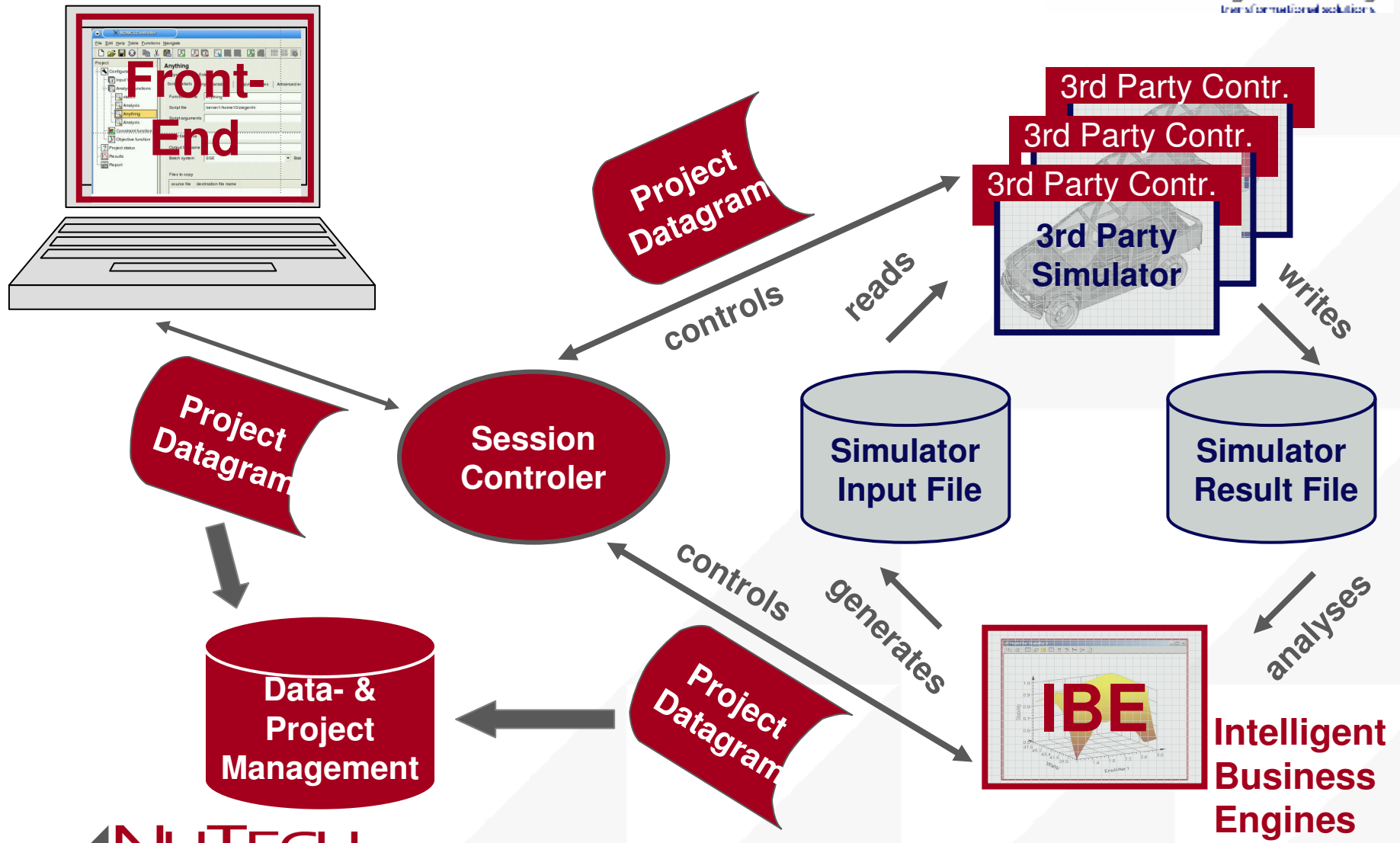
▲ the most efficient algorithms

&

▲ a robust and fail-safe environment

Requirements for a Tool

How it Works

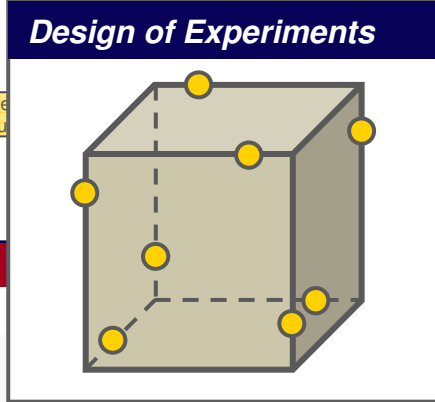
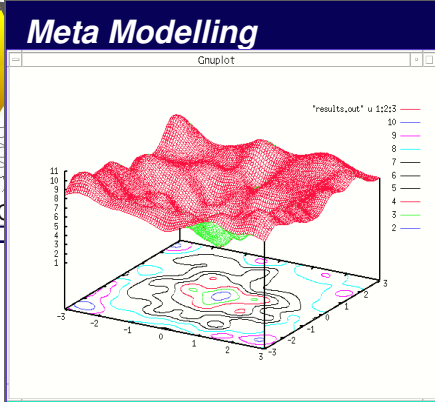
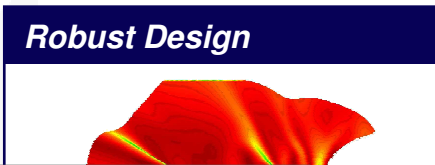
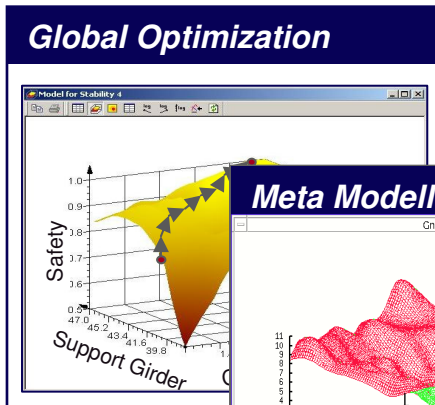


How it Works / IBEs

Computer Experiments

New Experiments

Experimental Results



Features and Architecture

Unique Features:

- ▲ Extensible XML-based Architecture
- ▲ Platform independent
- ▲ Runs 24/7 --- Hot-Plug Update
- ▲ Fast Adaptive Search
- ▲ Multi Criteria Design
- ▲ Thin Redundant Master
- ▲ ...

ClearVu Engineering

CV/E Kernel

Modules

CV/E
Global Optimization

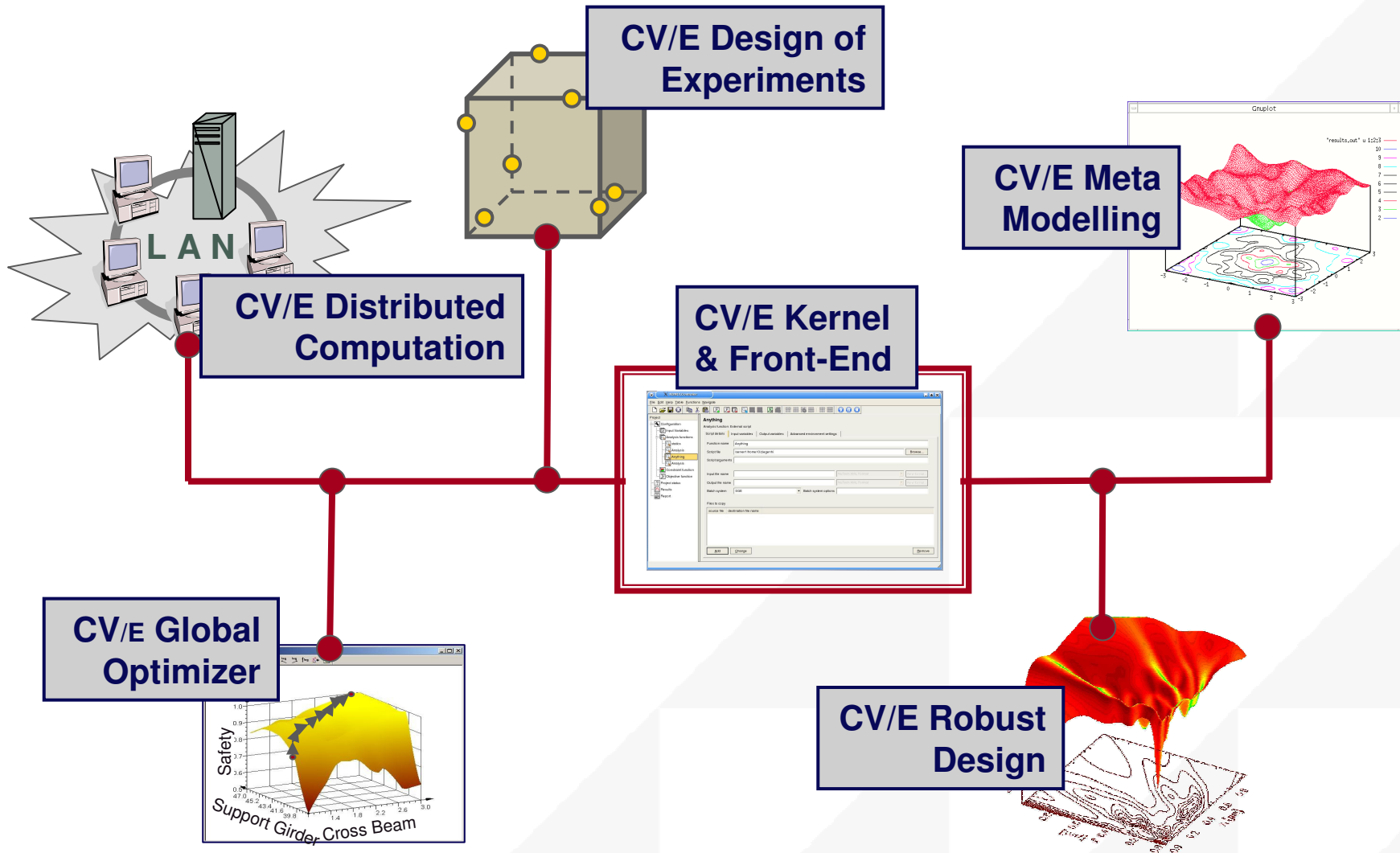
CV/E
Distributed Computation

CV/E
Design of Experiments

CV/E
Robust Design

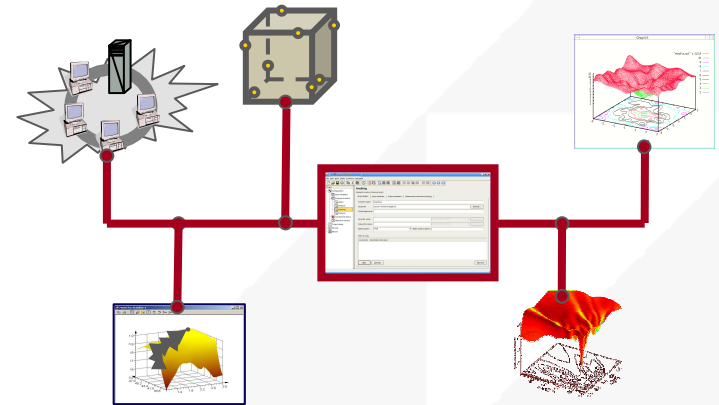
CV/E
Meta Modelling

Architecture

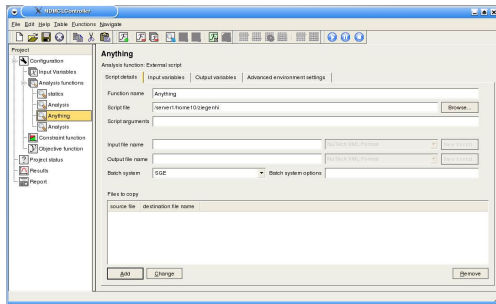


Unique Features

- ▲ Extensible XML-based Architecture
- ▲ Platform independent
- ▲ Runs 24/7 --- Hot-Plug Update
- ▲ Fast Adaptive Search
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- ▲ ...



The CV/E Kernel

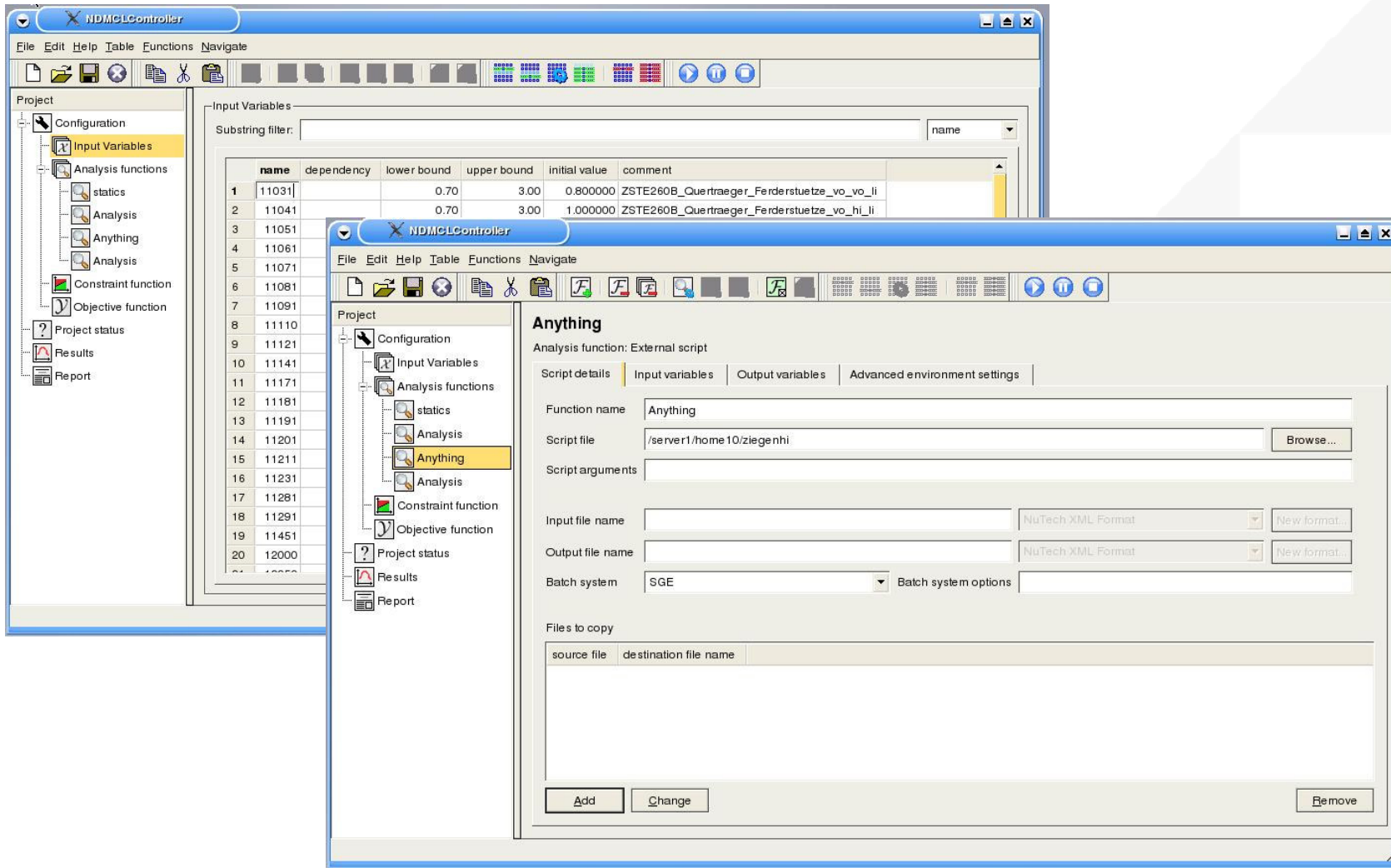


Features:

- ▲ **Modular Extensible Architecture**
- ▲ **Open to Integrate 3rd-Party Algorithms**
- ▲ **XML-Based Interfacing and API**
- ▲ **Simple to Use Graphical User Interface**
(& Optional Text Console)
- ▲ **Different Levels of User Skills and Permissions**
- ▲ **Project Templates Supporting Team Work**
- ▲ **Advanced Postprocessing†**

† available with release 2.2

Graphical User Interface



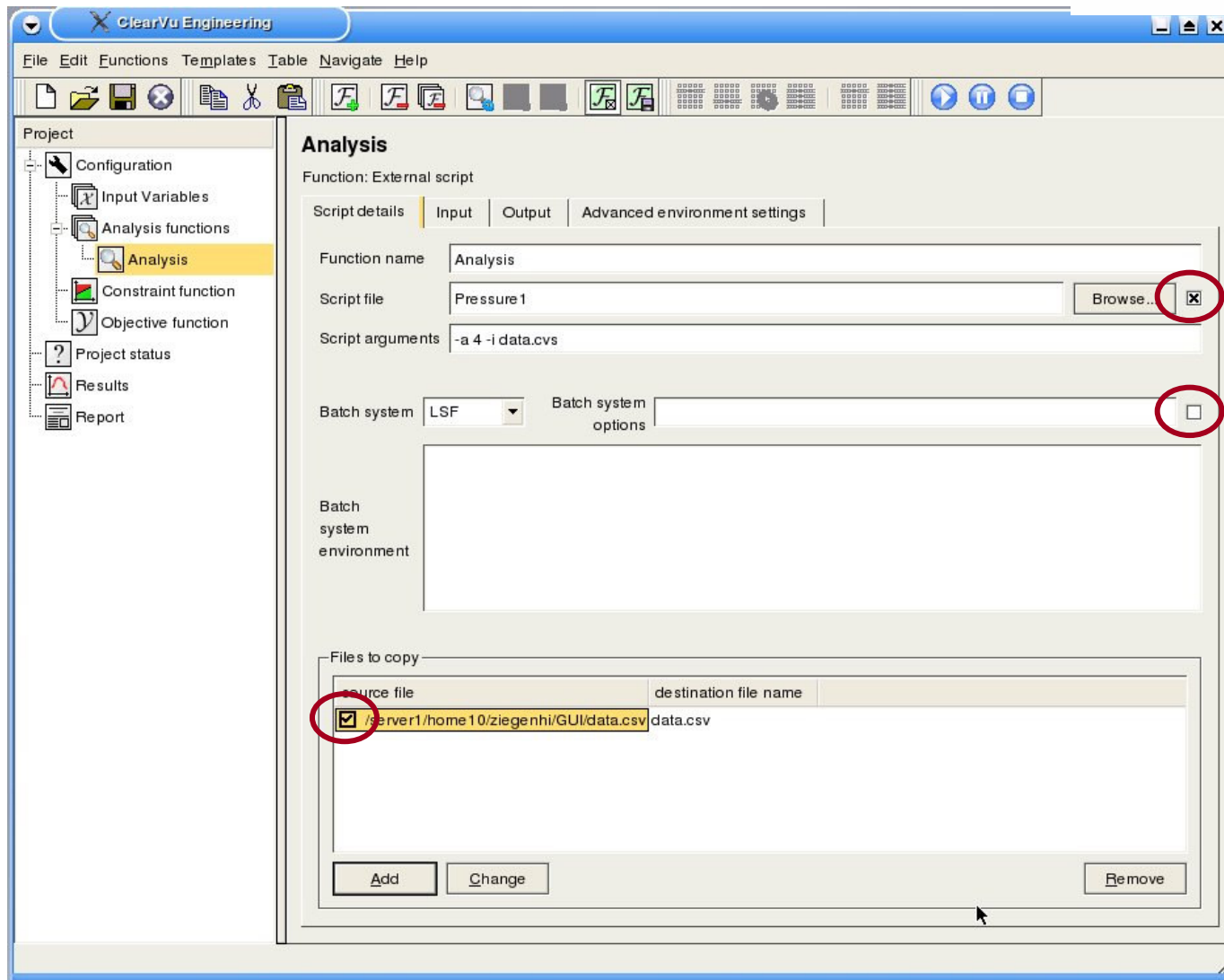
The screenshot displays the NDMCLController software interface. The main window is titled 'NDMCLController' and features a menu bar (File, Edit, Help, Table, Functions, Navigate) and a toolbar. On the left, a 'Project' tree view shows a hierarchy: Configuration, Input Variables, Analysis functions (with sub-items: statics, Analysis, Anything, Analysis), Constraint function, Objective function, Project status, Results, and Report. The 'Input Variables' section is active, showing a table with columns: name, dependency, lower bound, upper bound, initial value, and comment. The table contains 20 rows of data.

	name	dependency	lower bound	upper bound	initial value	comment
1	11031		0.70	3.00	0.800000	ZSTE260B_Quertraeger_Feederstuetze_vo_vo_li
2	11041		0.70	3.00	1.000000	ZSTE260B_Quertraeger_Feederstuetze_vo_hi_li
3	11051					
4	11061					
5	11071					
6	11081					
7	11091					
8	11110					
9	11121					
10	11141					
11	11171					
12	11181					
13	11191					
14	11201					
15	11211					
16	11231					
17	11281					
18	11291					
19	11451					
20	12000					

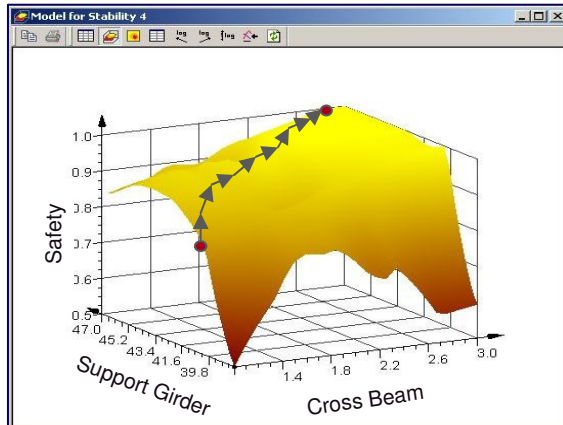
The 'Anything' analysis function configuration window is also shown, with tabs for Script details, Input variables, Output variables, and Advanced environment settings. The 'Script details' tab is active, showing fields for Function name (Anything), Script file (/server1/home10/ziege/nhi), Script arguments, Input file name, Output file name, Batch system (SGE), and Batch system options. A 'Files to copy' table is also present.

source file	destination file name
-------------	-----------------------

Project Templates



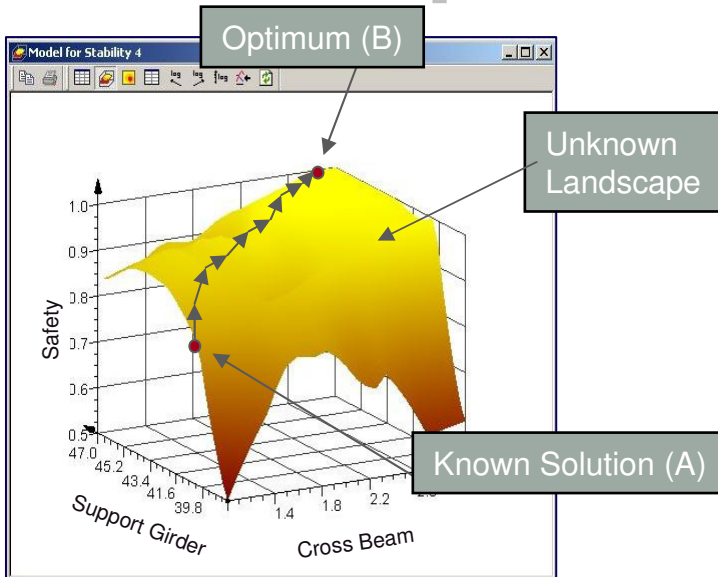
CV/E Global Optimizer



Features:

- ▲ Fast adaptive search
- ▲ Self-Adaptive Evolution Strategies
- ▲ Flexible constraint handling
- ▲ Handles infeasible initial solutions
- ▲ Variable degree of paralelism
- ▲ Multi criteria design
- ▲ Mode for the unexperienced users

Fast Adaptive Search

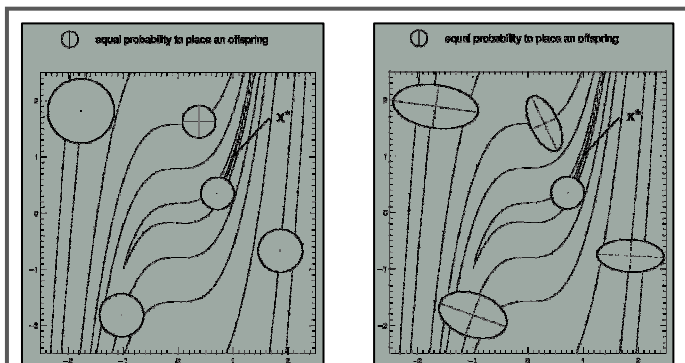


How to get

- ▲ from A to B (or equivalent solution)
- ▲ with high probability
- ▲ but minimal effort
- ▲ in an unknown landscape

Enhanced Evolution Strategies (ES)

- ▲ robust
- ▲ fast
- ▲ self-adaptive
- ▲ utilizes parallelism
- ▲ can deal with huge dimensions
- ▲ can deal with infeasible start designs
- ▲ can deal with mixed-integer spaces



Self-Adaptation of step sizes and directions

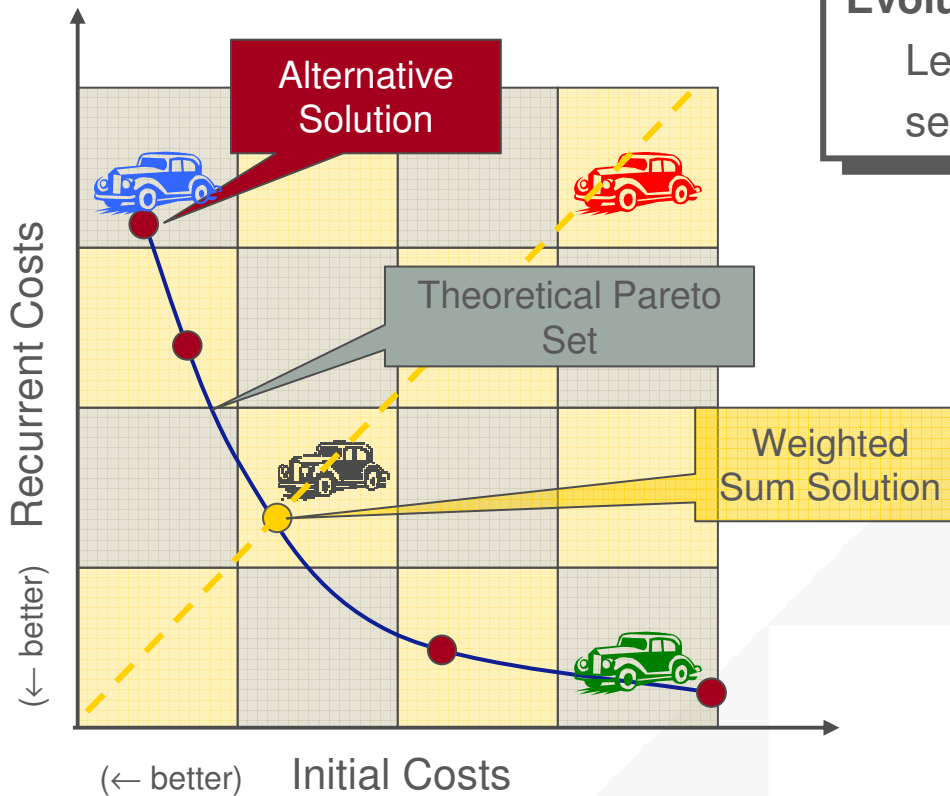
Multi Criteria Design

Multi Criteria Design:

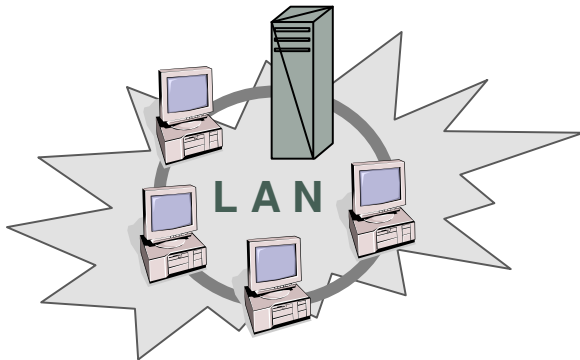
Find the whole set of optimal compromises

Evolutionary Multi Criteria Design:

Let the population of solutions represent the set of optimal compromises



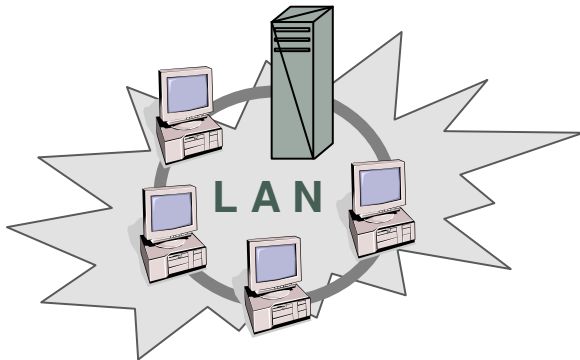
CV/E Distributed Computation



Features:

- ▲ Turns existing computer networks into robust computing cluster
- ▲ Improves access to computer farms
- ▲ Exploits inherent parallelism
- ▲ **Turns vulnerable hard/software environments into 24/7- systems**
- ▲ Eases administration of complex infrastructures
- ▲ Interfaces to 3rd-party batch-systems
- ▲ **Persistent Project Datagrams**
- ▲ Decentralized collaboration

CV/E Distributed Computation -2



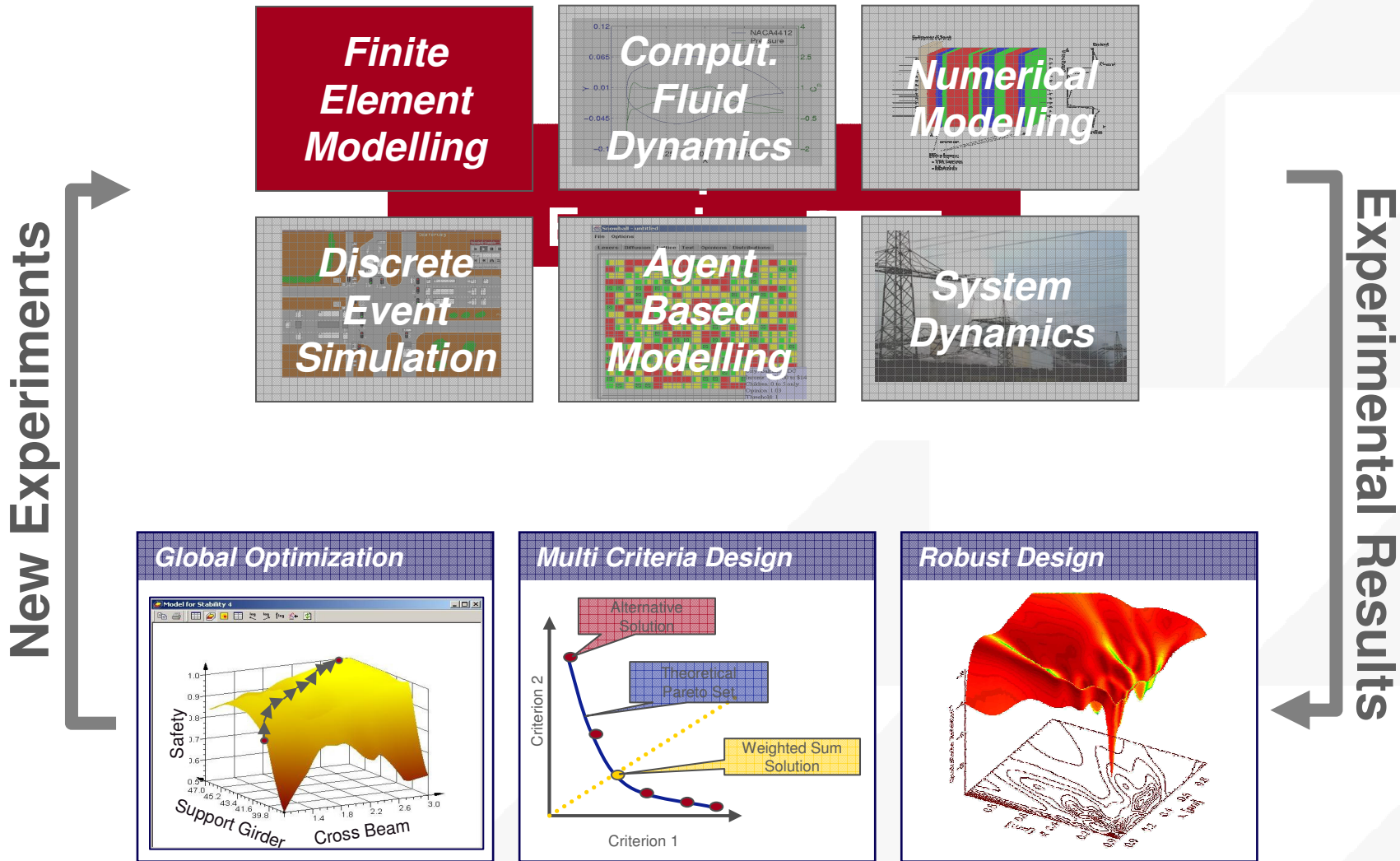
...

- ▲ **Redundant Thin Master architecture**
- ▲ Master operates independent of Front-Ends
- ▲ Distinguished Failure Reactions
- ▲ Advanced Data- and Projectmanagement
- ▲ Flexible Permissions-Scheme
- ▲ Hot-Plug Updates
- ▲ Supports Heterogenous Networks
- ▲ Process Monitoring †
- ▲ Simple Native Batch System†

† available with release 2.2

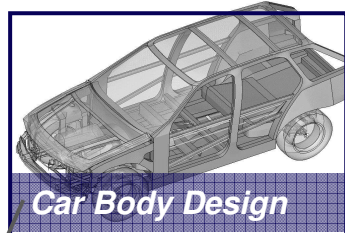
Some Examples

Application Map / FEM

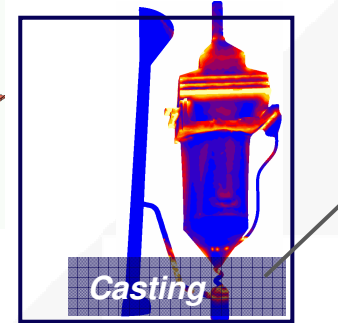
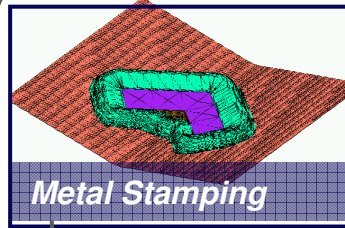


Application Map / FEM-2

Finite Element Modelling



Inflatable Knee Bolster



Optimal Casting Schedule for Turbine Blades

Safety Optimization – Pilot Study

- MDO Crash / Statics / Dynamics
- MCO B-Pillar Side Crash
- MCO Shape of Engine Mount

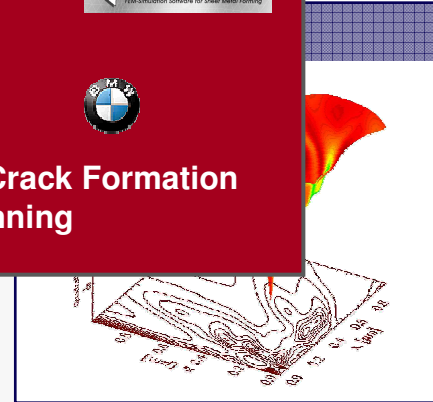
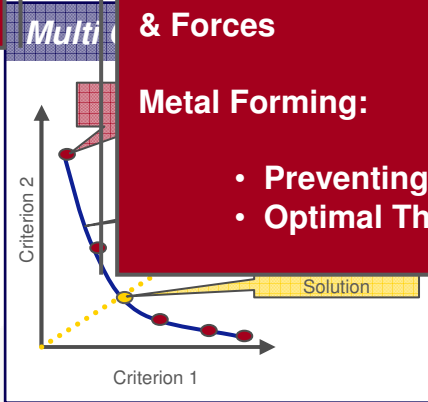
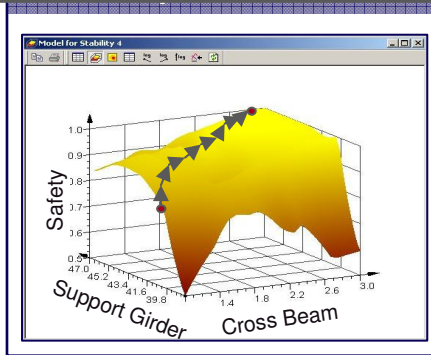
MDO Car Body Concept Phase

- MDO Crash / Statics / Dynamics

Geometric Parameters & Forces

Metal Forming:

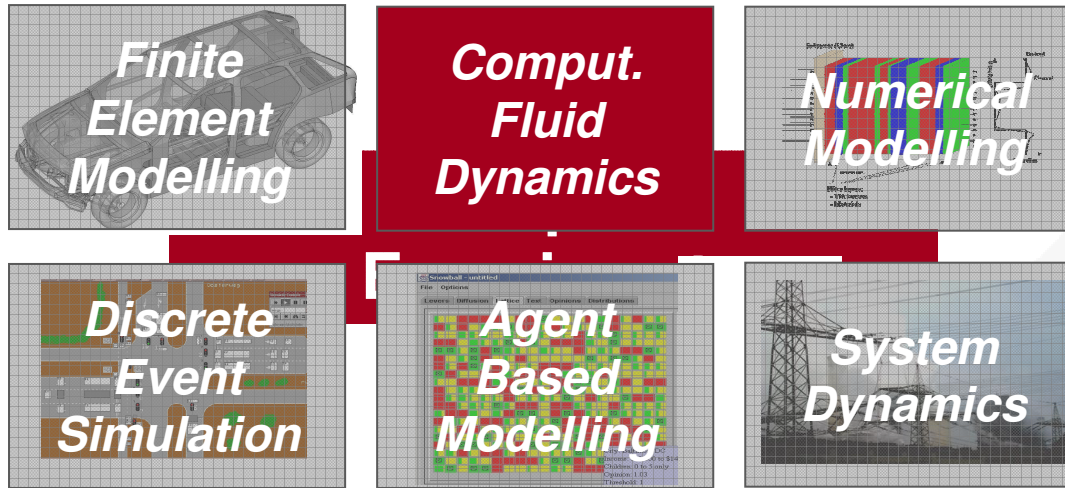
- Preventing Crack Formation
- Optimal Thinning



New

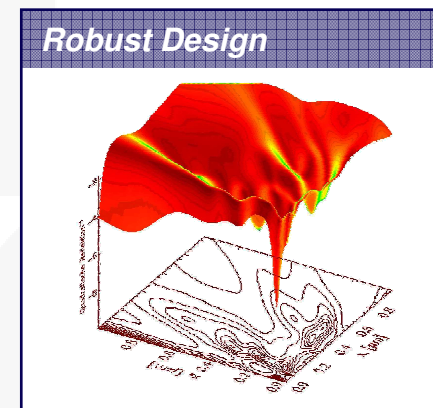
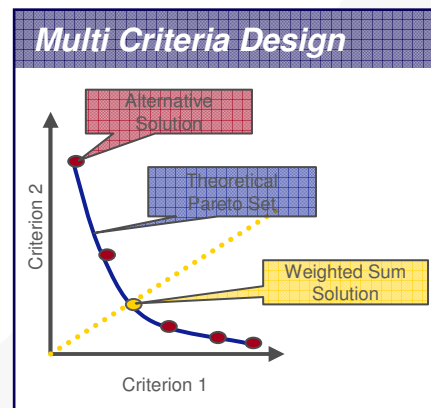
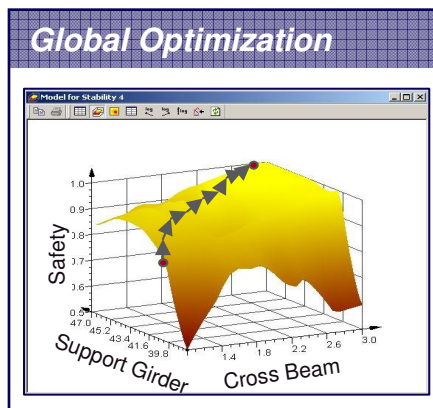
Expert
tal Results

Application Map / CFD

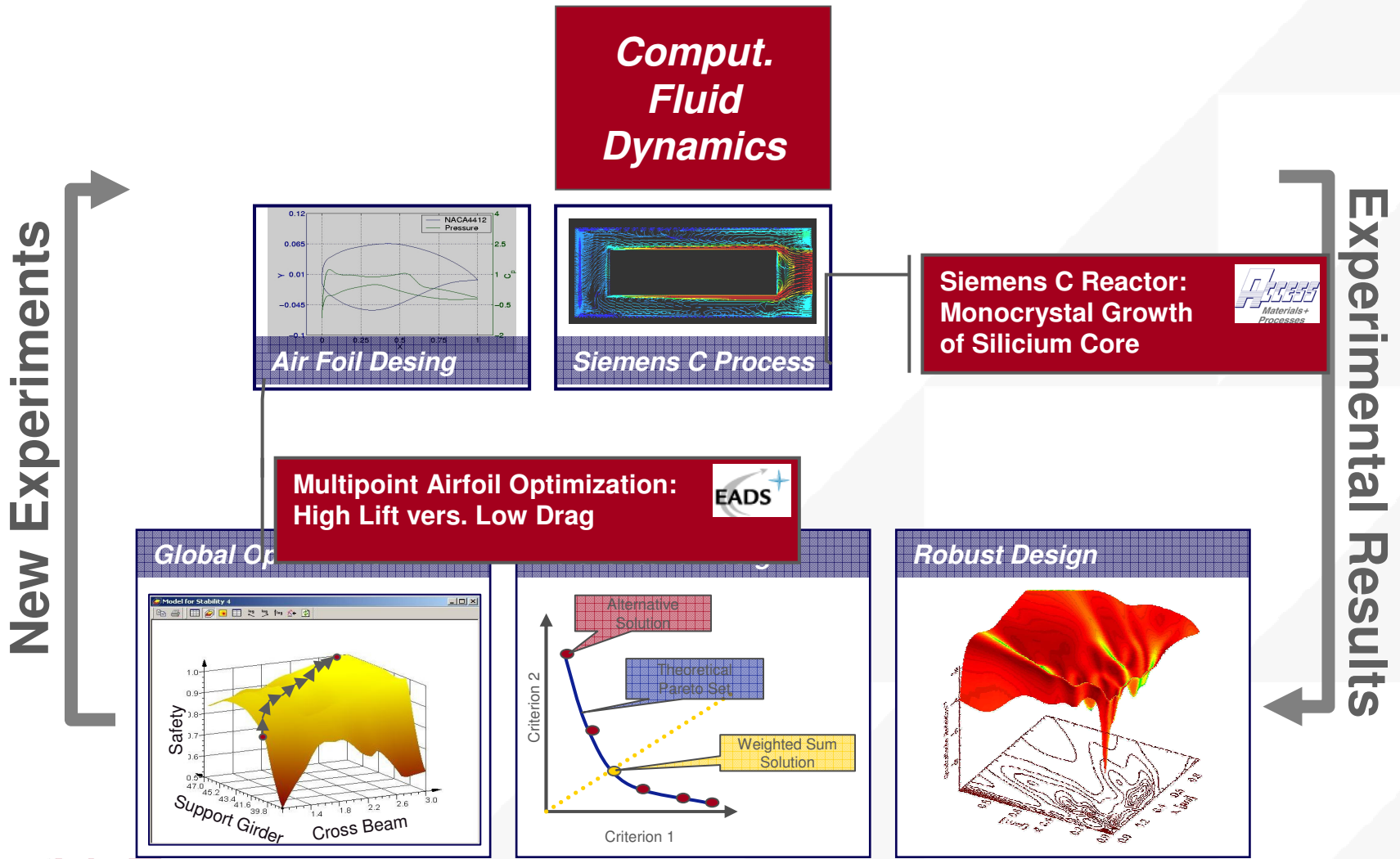


New Experiments

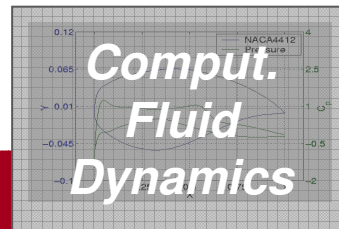
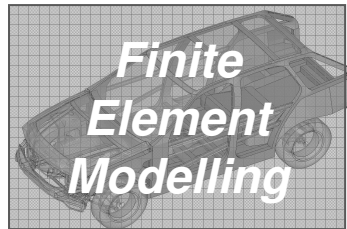
Experimental Results



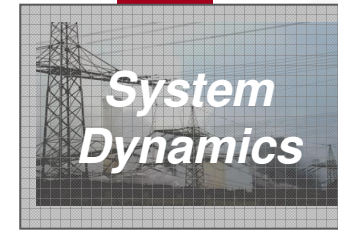
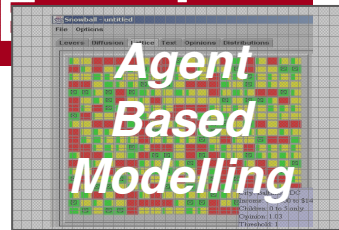
Application Map / CFD-2



Application Map / NM

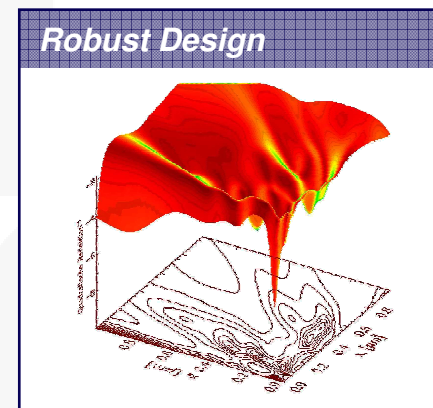
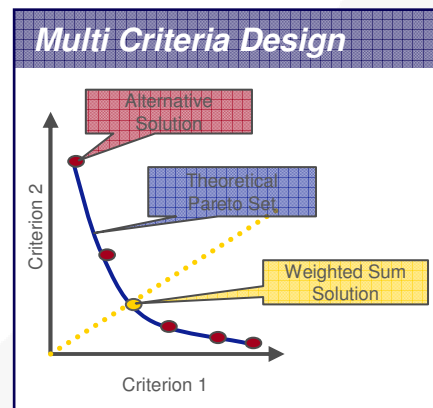
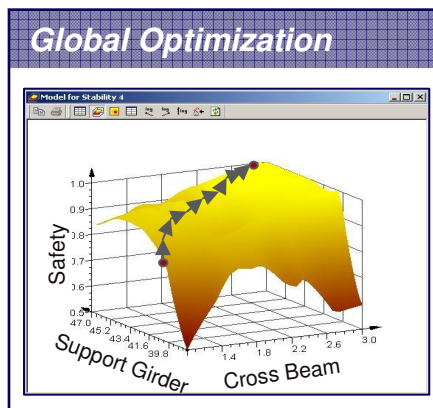


Numerical
Modelling



New Experiments

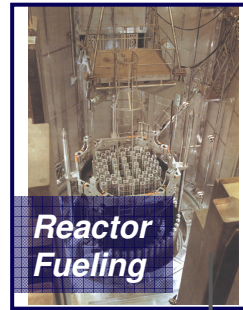
Experimental Results



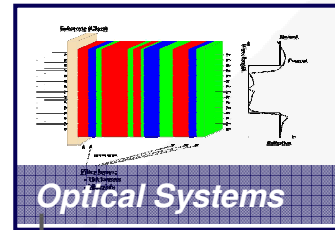
Application Map / NM-2

New Experiments

Experimental Results

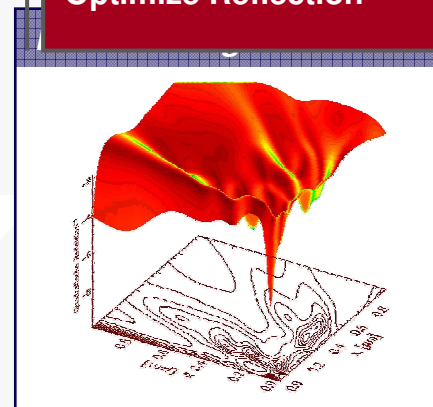
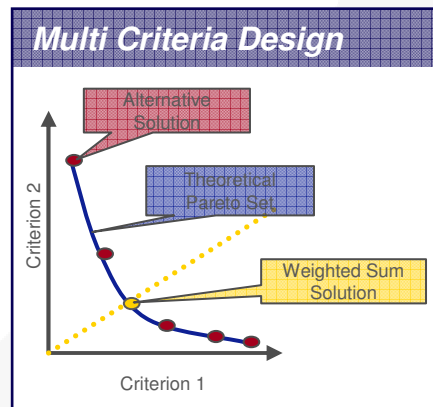
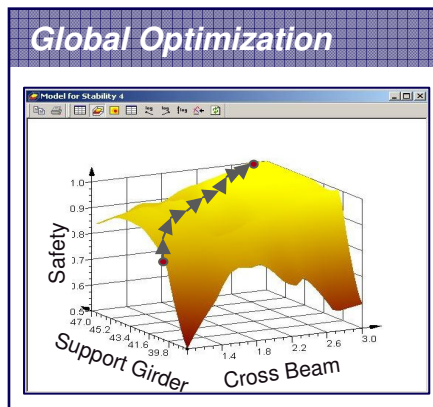


Numerical Modelling

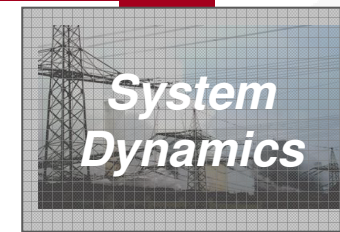
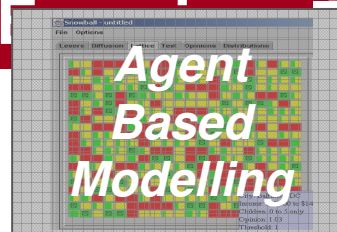
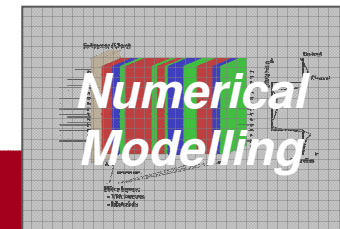
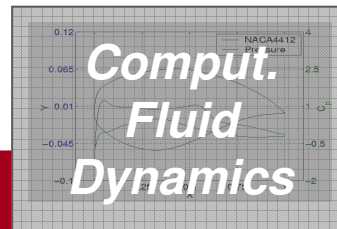
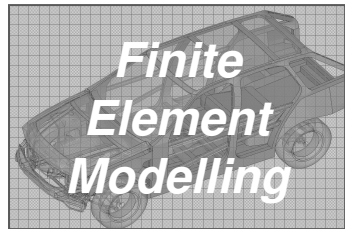


Optimize Fuel Assembly Reload Patterns **SIEMENS**

Optical Coatings: Optimize Reflection **CORNING**

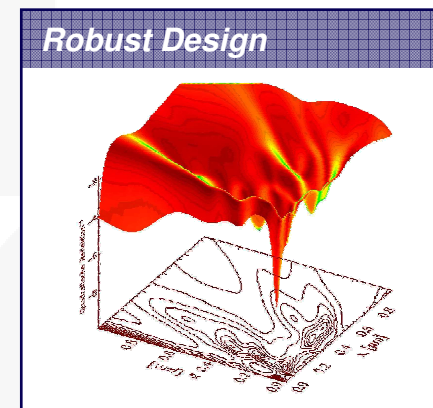
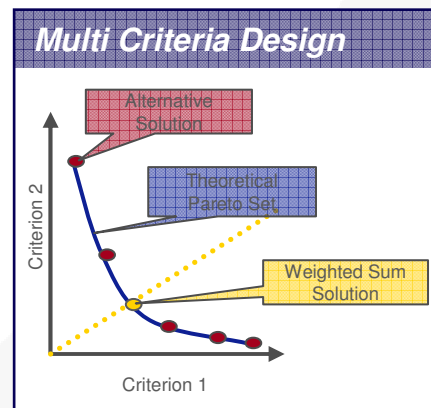
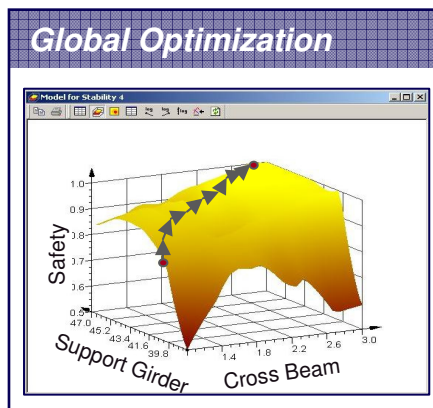


Application Map / DES



New Experiments

Experimental Results



Application Map / DES-2

Traffic Dependend
Dynamic Optimization



Ministerie van Verkeer en Waterstaat

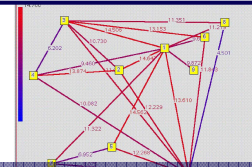
Routing Table
Optimization

SIEMENS

*Discrete
Event
Simulation*



Traffic Control

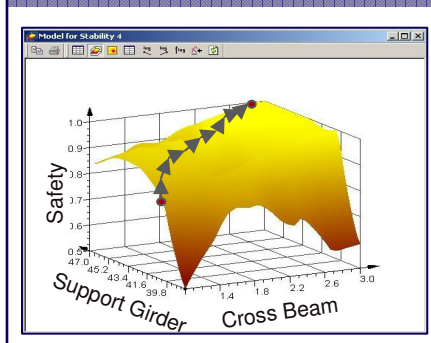


Comm. Networks

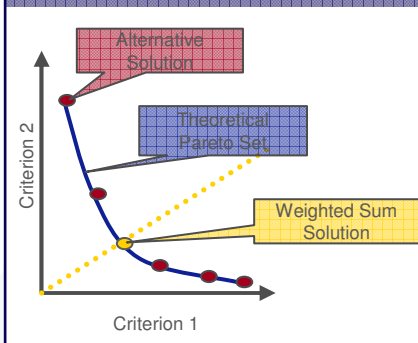
New Experiments

Experimental Results

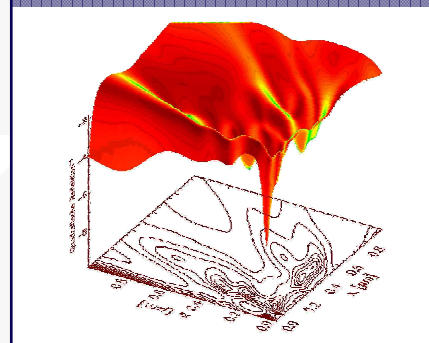
Global Optimization



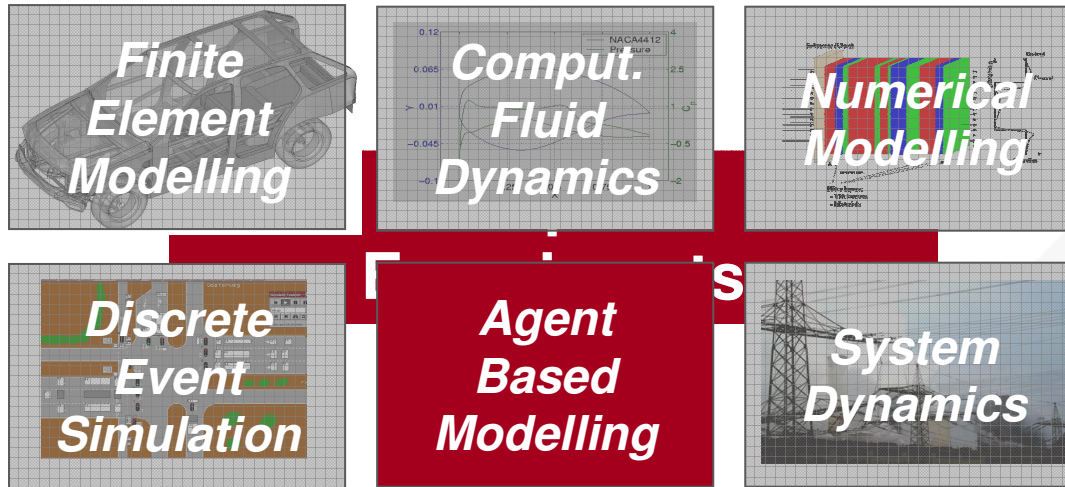
Multi Criteria Design



Robust Design

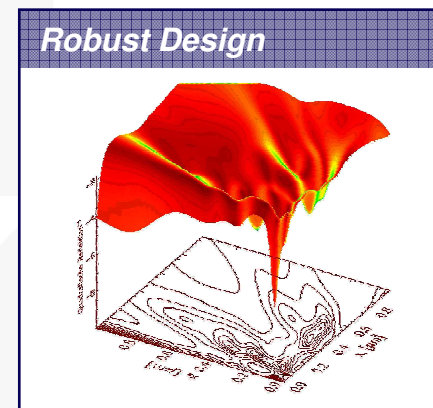
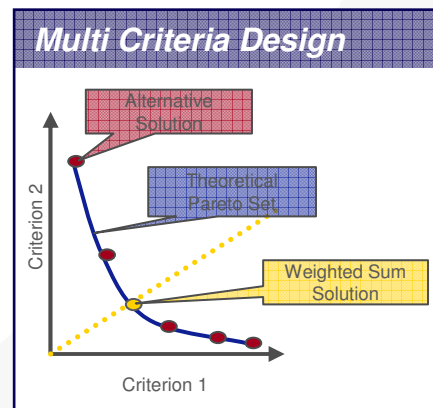
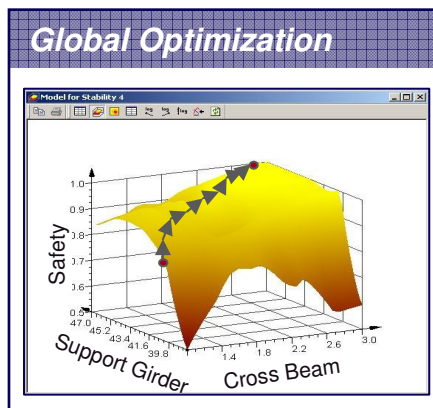


Application Map / ABM



New Experiments

Experimental Results

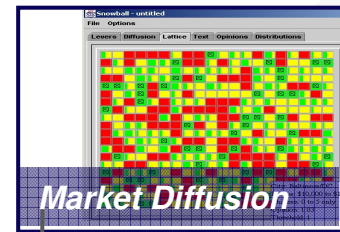


Application Map / ABM-2

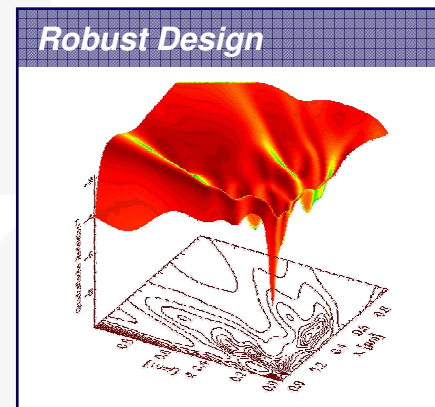
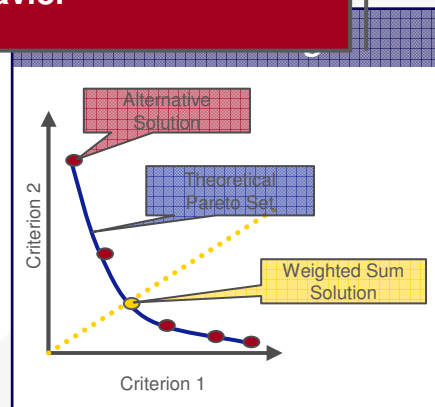
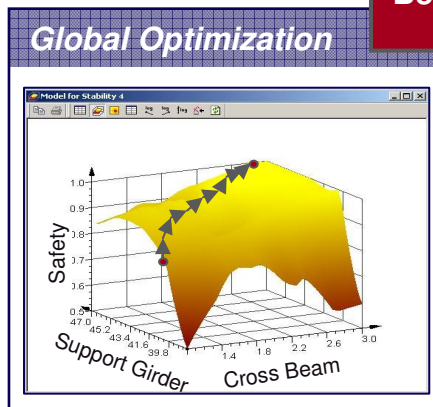
New Experiments

Experimental Results

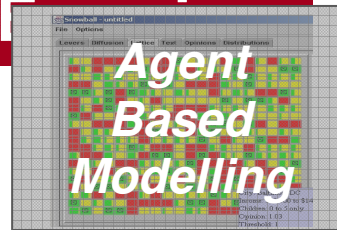
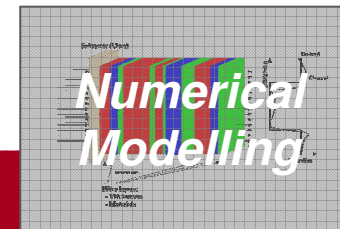
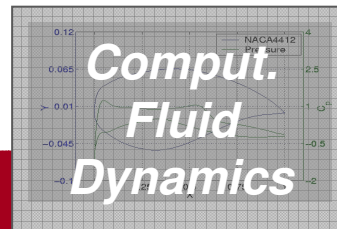
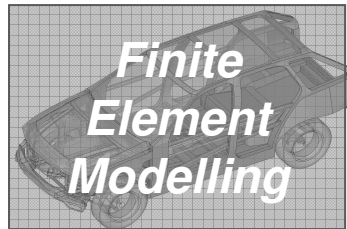
Agent Based Modelling



Modelling Consumer Behavior

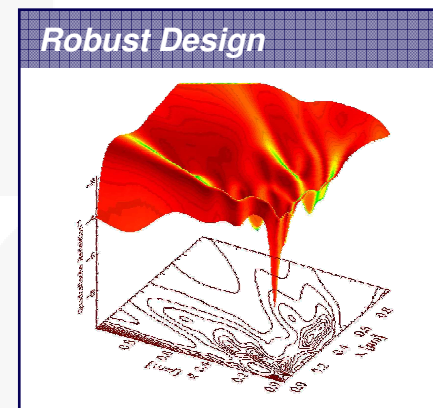
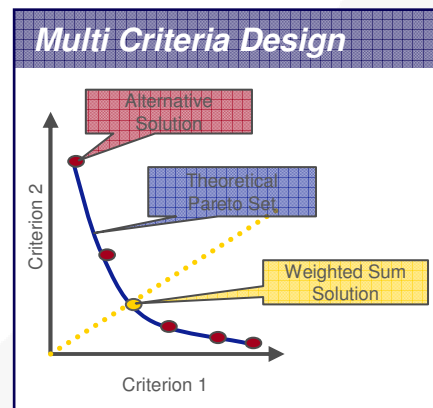
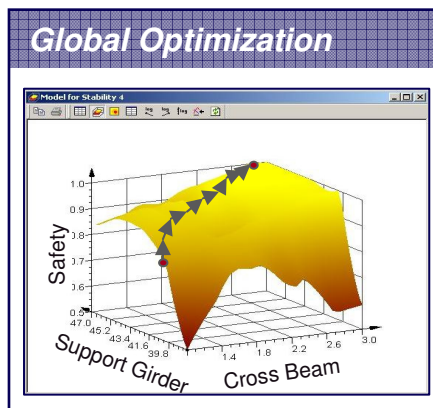


Application Map / SD



New Experiments

Experimental Results



Application Map / SD-2

Corporate Planning:



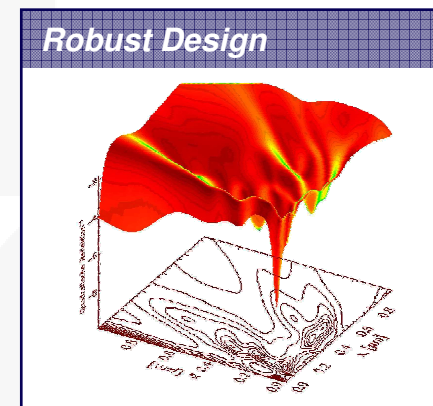
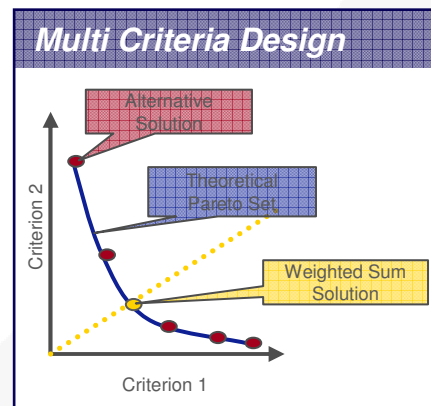
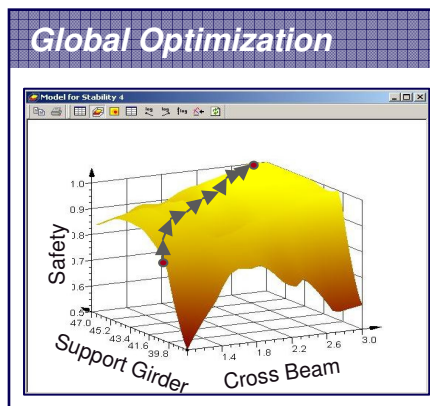
- Capacity Planning; Very Large Time Scales
- Price Dynamics
- CO₂ - Trading



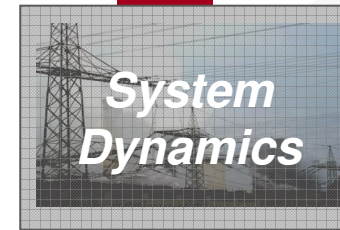
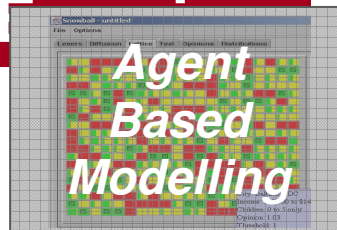
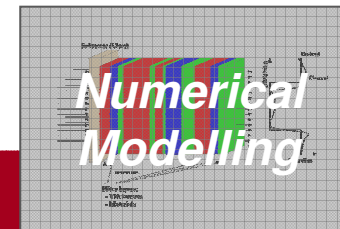
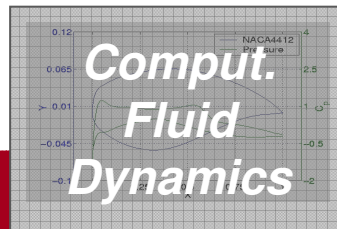
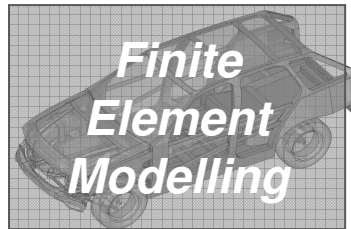
**System
Dynamics**

Experimental Results

New Ex

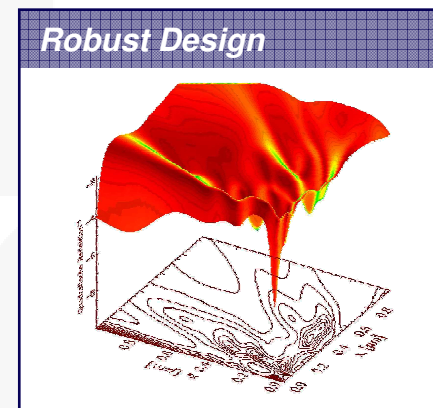
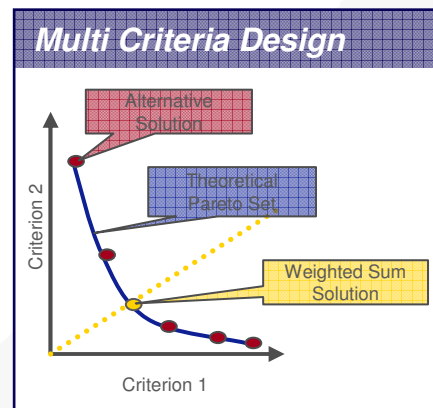
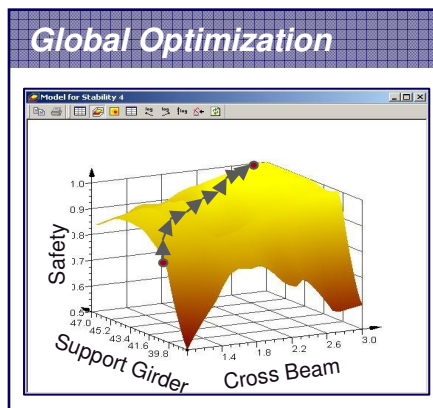


Application Map / End



New Experiments

Experimental Results



Engineering Optimization

Optimization Creating Innovation

▲ Illustrative Example: Optimize Efficiency

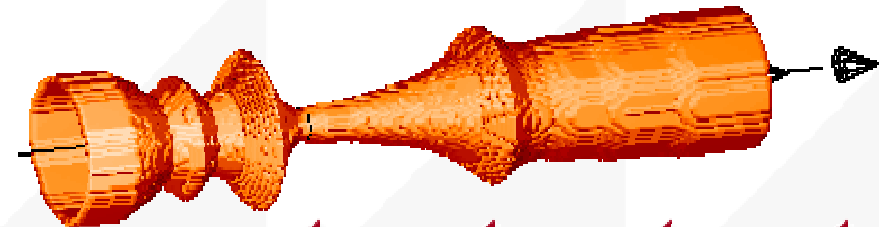
▲ Initial:



▲ Evolution:



▲ 32% Improvement in Efficiency !



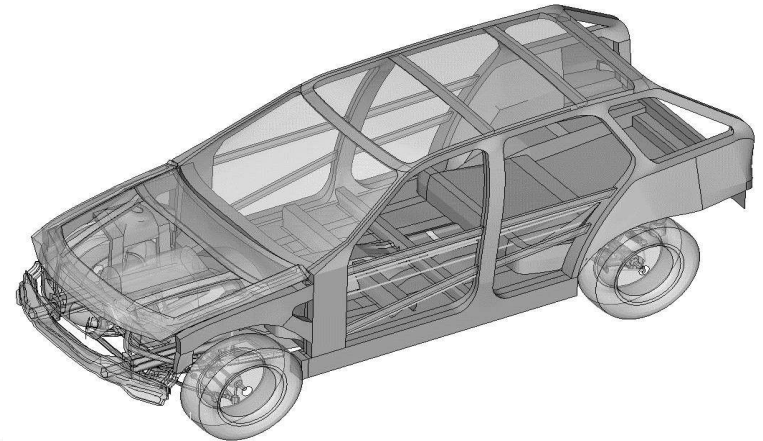
Safety Optimization – Pilot Study



- ▲ Aim: Identification of most appropriate Optimization Algorithm for realistic example!
- ▲ Optimizations for 3 test cases and 14 algorithms were performed ($28 \times 10 = 280$ shots)
 - ▲ Body MDO Crash / Statics / Dynamics
 - ▲ MCO B-Pillar
 - ▲ MCO Shape of Engine Mount
- ▲ NuTech's ES performed significantly better than Monte-Carlo-scheme, GA, and Simulated Annealing
- ▲ Results confirmed by statistical hypothesis testing

MDO Crash / Statics / Dynamics

- ▲ Minimization of body mass
- ▲ Finite element mesh
 - ▲ Crash ~ 130.000 elements
 - ▲ NVH ~ 90.000 elements
- ▲ Independent parameters:
Thickness of each unit: 109
- ▲ Constraints: 18



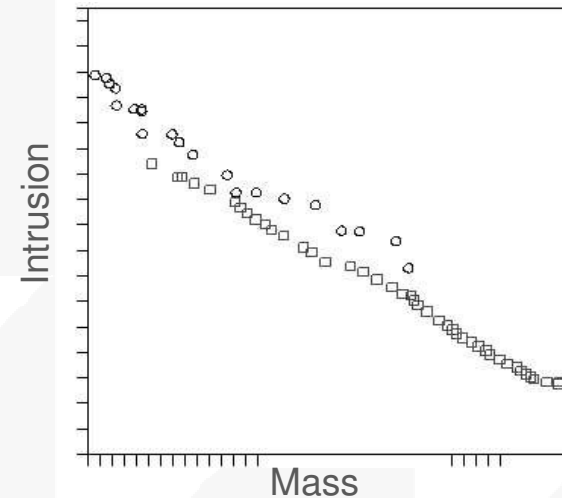
Algorithm	Avg. reduction (kg)	Max. reduction (kg)	Min. reduction (kg)
Best so far	-6.6	-8.3	-3.3
NuTech ES	-9.0	-13.4	-6.3

MCO B-Pillar – Side Crash



- ▲ Minimization of mass & displacement
- ▲ Finite element mesh
 - ▲ ~ 300.000 elements
- ▲ Independent parameters:
Thickness of 10 units
- ▲ Constraints: 0

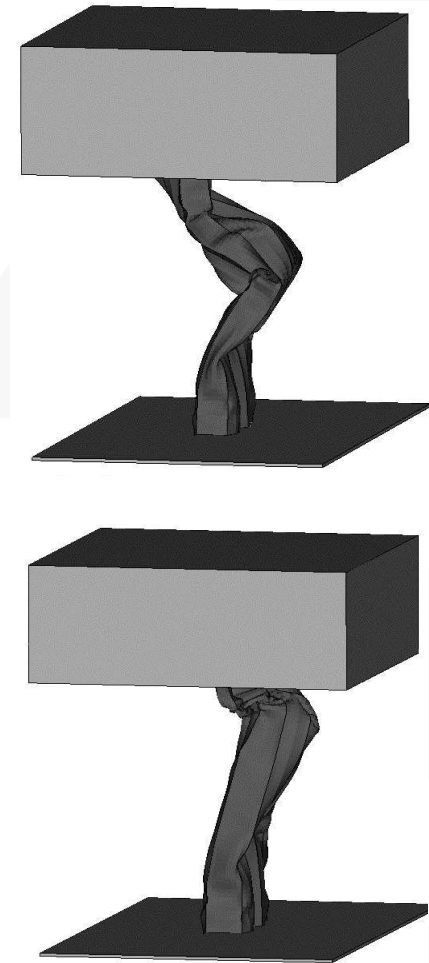
- ▲ ES successfully developed Pareto front



MCO Shape of Engine Mount



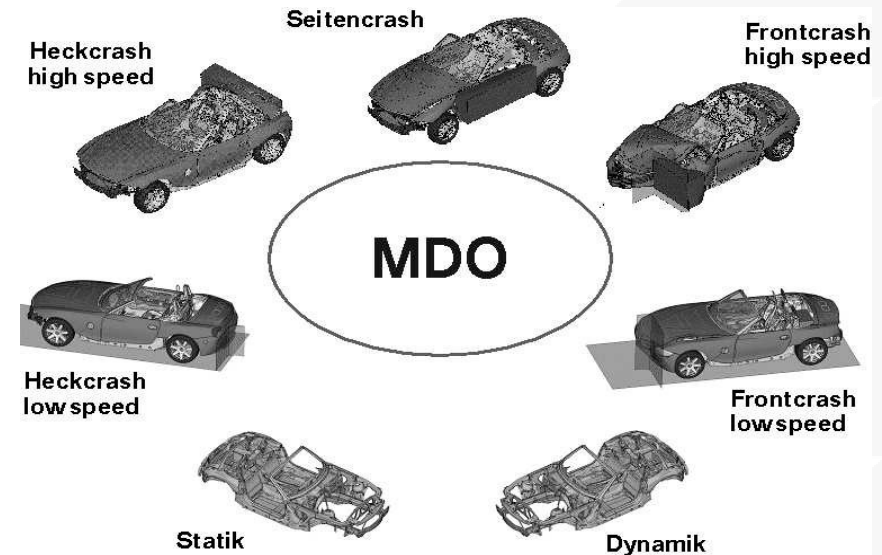
- ▲ Mass minimal shape with axial load > 90 kN
- ▲ Finite element mesh
 - ▲ ~ 5000 elements
- ▲ Independent parameters: 9 geometry variables
- ▲ Dependent parameters: 7
- ▲ Constraints: 3
- ▲ ES optimized mount
 - ▲ less weight than mount optimized with best so far method
 - ▲ geometrically better deformation



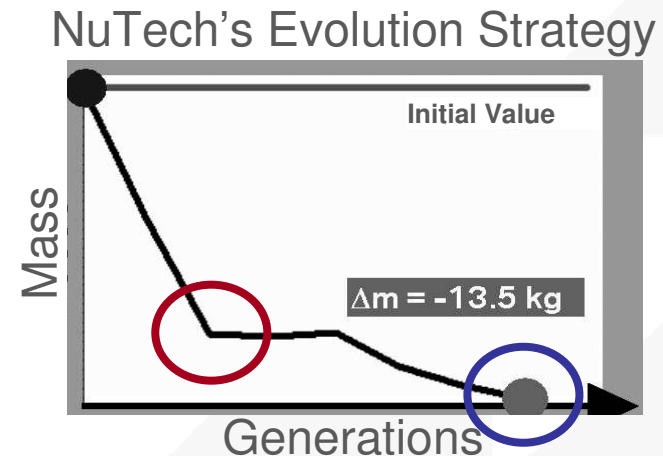
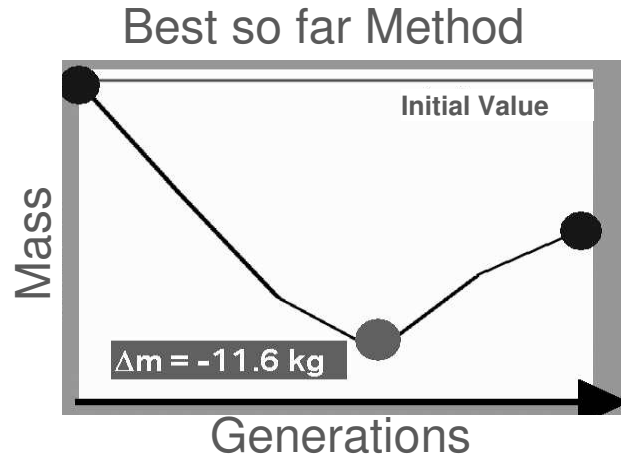
Safety Optimization – Example of use



- ▲ Production Run !
- ▲ Minimization of body mass
- ▲ Finite element mesh
 - ▲ Crash ~ 1.000.000 elements
 - ▲ NVH ~ 300.000 elements
- ▲ Independent parameters:
 - ▲ Thickness of each unit: 136
- ▲ Constraints: 47, resulting from various loading cases
- ▲ 180 (10 x 18) shots ~ 12 days
- ▲ No statistical evaluation due to problem complexity



Safety Optimization – Example of use



- ▲ 13,5 kg weight reduction by NuTech's ES
- ▲ ~ 2 kg more mass reduction than Best so far method
- ▲ Typically higher convergence velocity of ES
 - ~ 45% less time (~ 3 days saving) for comparable quality needed
- ▲ Still potential of improvements after 180 shots.
- ▲ Reduction of development time from 5 to 2 weeks allows for process integration

Mixed-Integer Evolution Strategies

Mixed-Integer Evolution Strategy

▲ Optimization Task Definition:

$$f(r_1, \dots, r_{n_r}, z_1, \dots, z_{n_z}, d_1, \dots, d_{n_d}) \rightarrow \min$$

subject to:

$$r_i \in [r_i^{\min}, r_i^{\max}] \subset \mathbb{R}, \quad i = 1, \dots, n_r$$

$$z_i \in [z_i^{\min}, z_i^{\max}] \subset \mathbb{Z}, \quad i = 1, \dots, n_z$$

$$d_i \in D_i = \{d_{i,1}, \dots, d_{i,|D_i|}\}, \quad i = 1, \dots, n_d$$

Mixed-Integer Evolution Strategy

Mutation operator:

```
for  $i = 1, \dots, n_r$  do
   $s'_i \leftarrow s_i \exp(\tau_g N_g + \tau_l N(0, 1))$ 
   $r'_i = r_i + N(0, s'_i)$ 
end for
for  $i = 1, \dots, n_z$  do
   $q'_i \leftarrow q_i \exp(\tau_g N_g + \tau_l N(0, 1))$ 
   $z'_i \leftarrow z_i + G(0, q'_i)$ 
end for
 $p'_i := 1 / [1 + \frac{1-p_i}{p_i} * \exp(-\tau_l * N(0, 1))]$ 
for  $i \in \{1, \dots, n_d\}$  do
  if  $U(0, 1) < p'_i$  then
     $d'_i \leftarrow$  uniformly randomly value from  $D_i$ 
  end if
end for
```

Learning rates
(global)

Learning rates
(local)

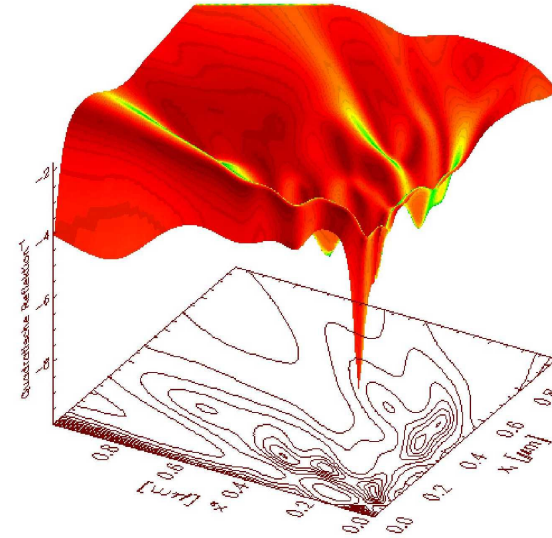
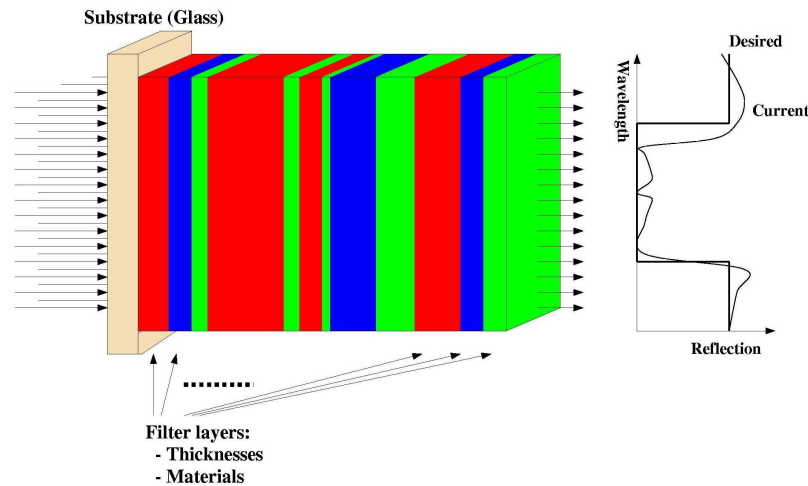
Geometrical
distribution

Mutation
probabilities

Application Examples



Example: Optical Coating Design



- ▲ Nonlinear, mixed-integer
- ▲ Variable dimensionality
- ▲ Minimize deviation from desired performance
- ▲ Excellent synthesis method

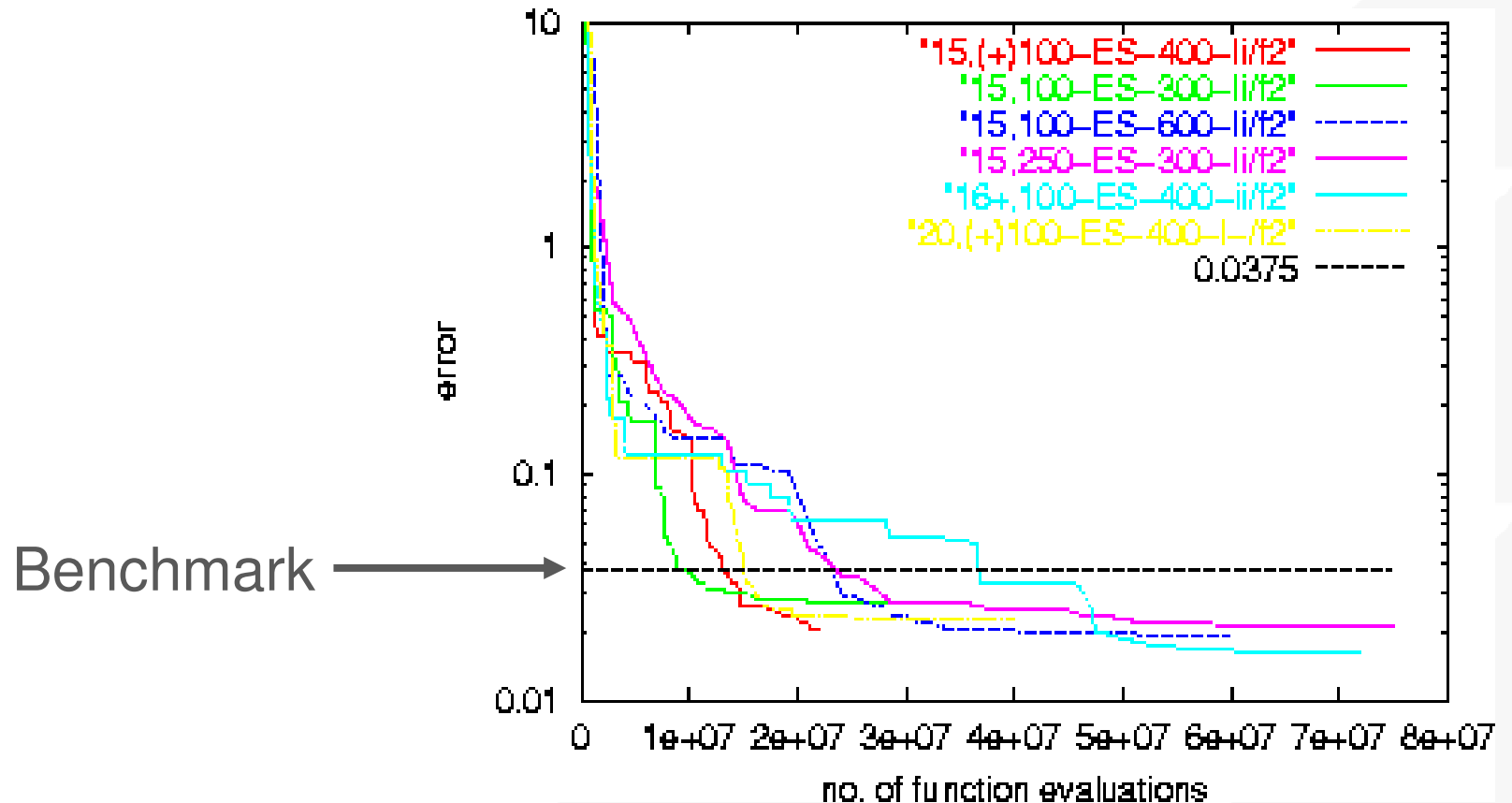
Example: Optical Coating Design



$$quality = \sum_{i=1}^{15} weight_i \cdot \left(\frac{calculated_i - desired_i}{scale_i} \right)^2 \rightarrow \min$$

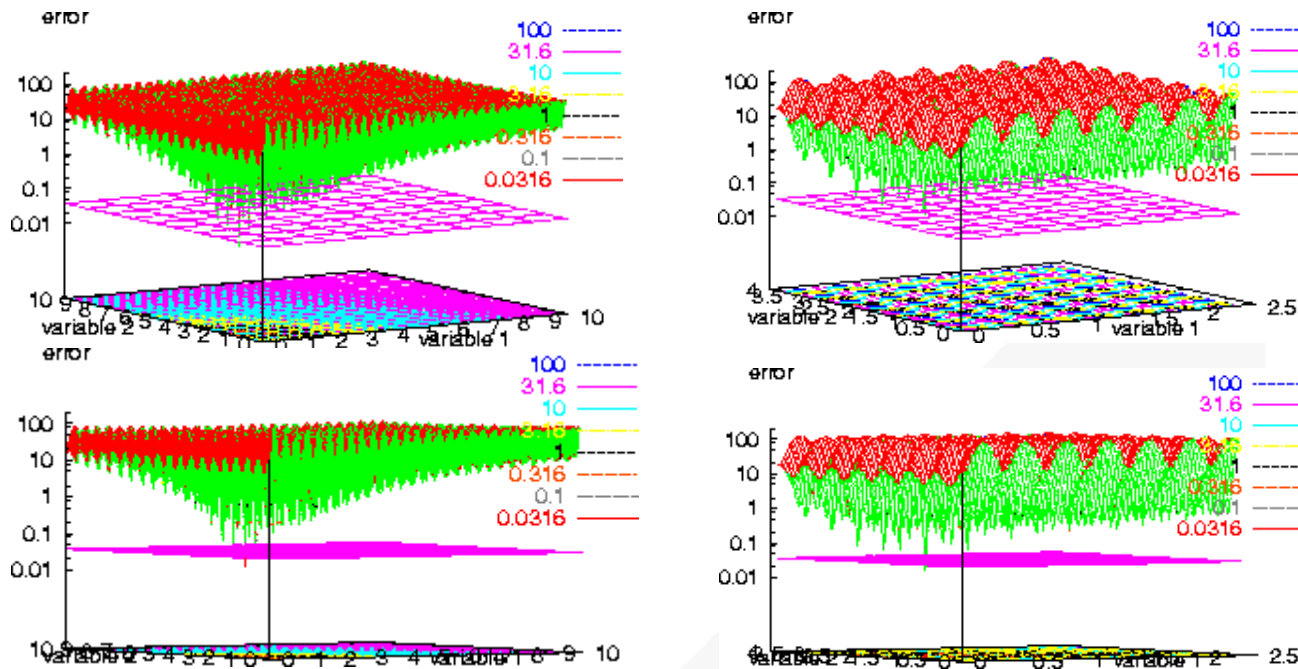
- ▲ Dielectric filter design
- ▲ $n=40$ layers
- ▲ Layer thicknesses x_i in $[0.01, 10.0]$
- ▲ Quality: Sum of quadratic penalty terms

Example: Results



- ▲ Factor 2 in quality, 10 in effort !
- ▲ Reliable, repeatable results

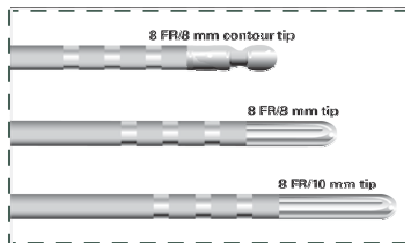
Example: Problem Topology



▲ Vicinity of global optimum

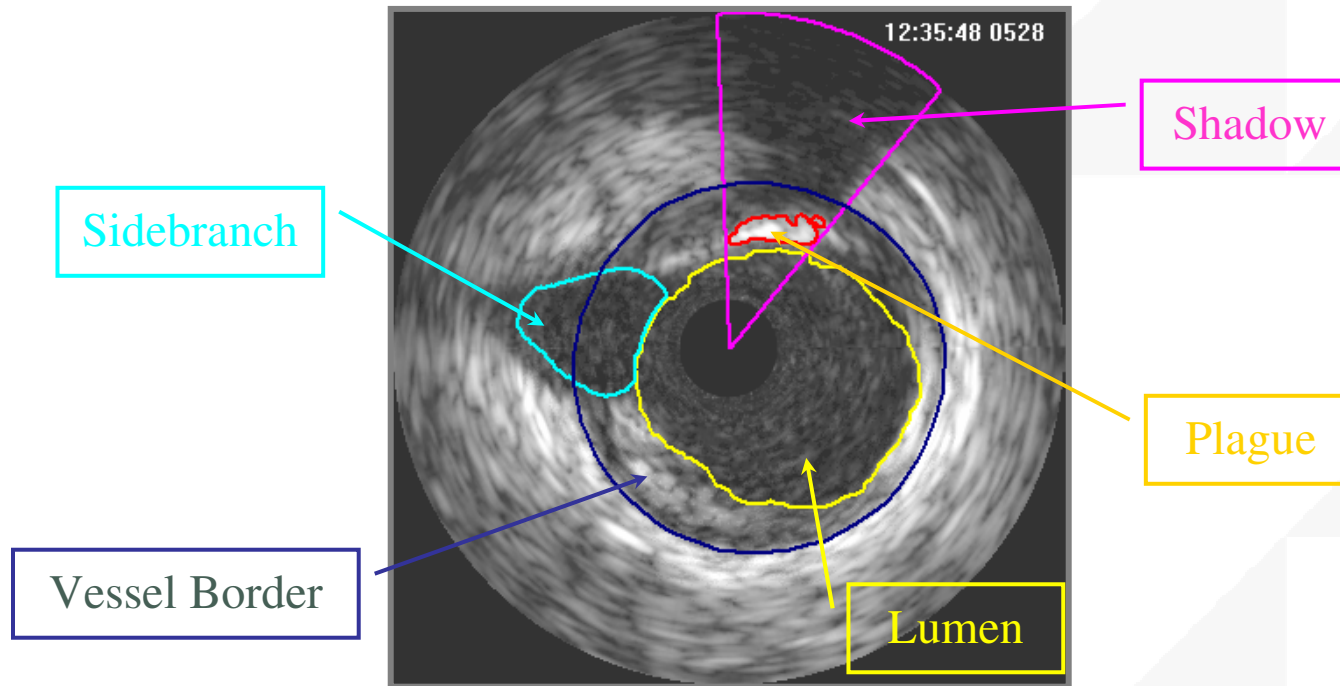
Example: Intravascular Ultrasound Image Analysis

- Real-time high-resolution tomographic images from the inside of coronary vessels:



Intravascular Ultrasound Image Analysis

▲ Detected Features in an IVUS Image:



Experimental Results on IVUS images

Parameters for the lumen feature detector

name	type	range	dependencies	default
maxgray	integer	[2, 150]	> mingray	35
mingray	integer	[1, 149]	< maxgray	1
connectivity	ordinal	4,6,8		6
relativeopenings	boolean	{false,true}		true
nrofcloses	integer	[0, 100]	used if not relativeopenings	5
nrofopenings	integer	[0, 100]	used if not relativeopenings	45
scanlinedir	ordinal	{0,1,2}		1
scanindexleft	integer	[-100, 100]	< scanindexright	-55
scanindexright	integer	[-100, 100]	> scanindexleft	7
centermethod	ordinal	{0,1}		1
fitmodel	ordinal	{ellipse, circl}		ellipse
sigma	continuous	[0.5 10.0]		0.8
scantype	ordinal	{0,1,2}		0
sidestep	integer	[0, 20]		3
sidecost	continuous	[0.0, 100]		5
nroflines	integer	[32, 256]		128

Intravascular Ultrasound Image Analysis: Results

- On each of 5 data sets algorithm ran for 2804 evaluations – 19,5h of total computing time

dataset	default parameters		parameter solution 1		parameter solution 2		parameter solution 3		parameter solution 4		parameter solution 5	
	fitness	s.d.	fitness	s.d.	fitness	s.d.	fitness	s.d.	fitness	s.d.	fitness	s.d.
1	395.2	86.2	148.4	39.5	159.8	43.5	185.4	43.0	144.8	42.0	271.0	74.8
2	400.2	109.2	183.3	59.2	180.7	58.4	207.2	69.2	232.7	71.0	352.0	73.1
3	344.8	65.6	205.9	69.8	203.9	70.1	164.4	49.7	183.9	80.3	327.1	55.9
4	483.1	110.6	284.4	92.7	269.0	73.2	250.4	80.4	173.2	64.7	330.1	82.2
5	444.2	90.6	368.4	100.9	370.9	102.5	462.2	377.3	168.7	64.0	171.8	54.5

Performance of the best found MI-ES parameter solutions

- A paired two-tailed t-test was performed on the difference measurements for each image dataset using a 95% confidence interval ($p=0.05$)
- The null-hypothesis is that the mean difference results of the best MI-ES individual and the default parameters are equal.

- Significant improvement over expert tuning

Other Examples



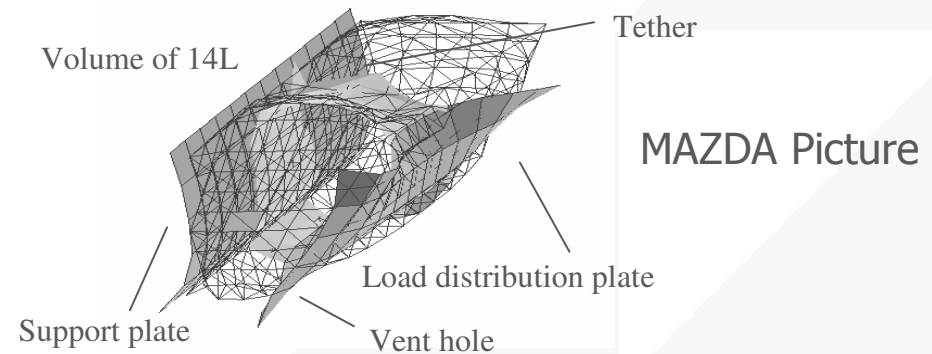
Inflatable Knee Bolster

Objective: Minimize $P_{combined}$

Subject to: Left Femur load ≤ 7000
Right Femur load ≤ 7000

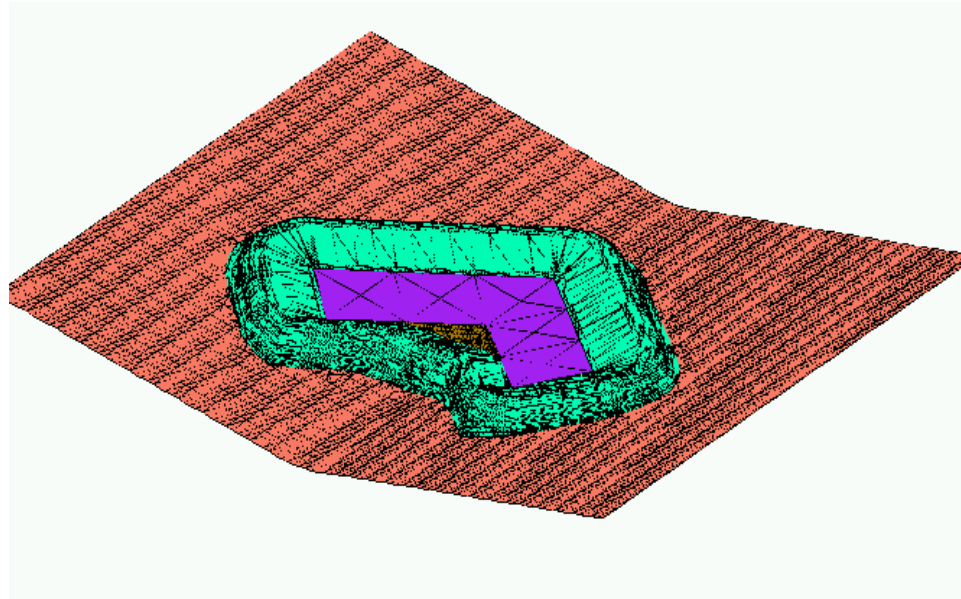
Design Variable
IKB center offset x
IKB center offset y
KB venting area ratio
KB mass inflow ratio
DB venting area ratio
DB high output mass inflow ratio
DB low output mass inflow ratio
DB firing time
DB strap length ratio
Load of load limiter (N)
Performance Response
HIC
CG
Left foot load
Right foot load
$P_{combined}$ (Quality)

deployed knee bag (unit only)



Design	$P_{combined}$	# Simulations
Base	13.69	--
Hooke Jeeves	8.89	160
GA (Ford)	7.29	155
ES	6.77	122

Optimization of metal stamping process

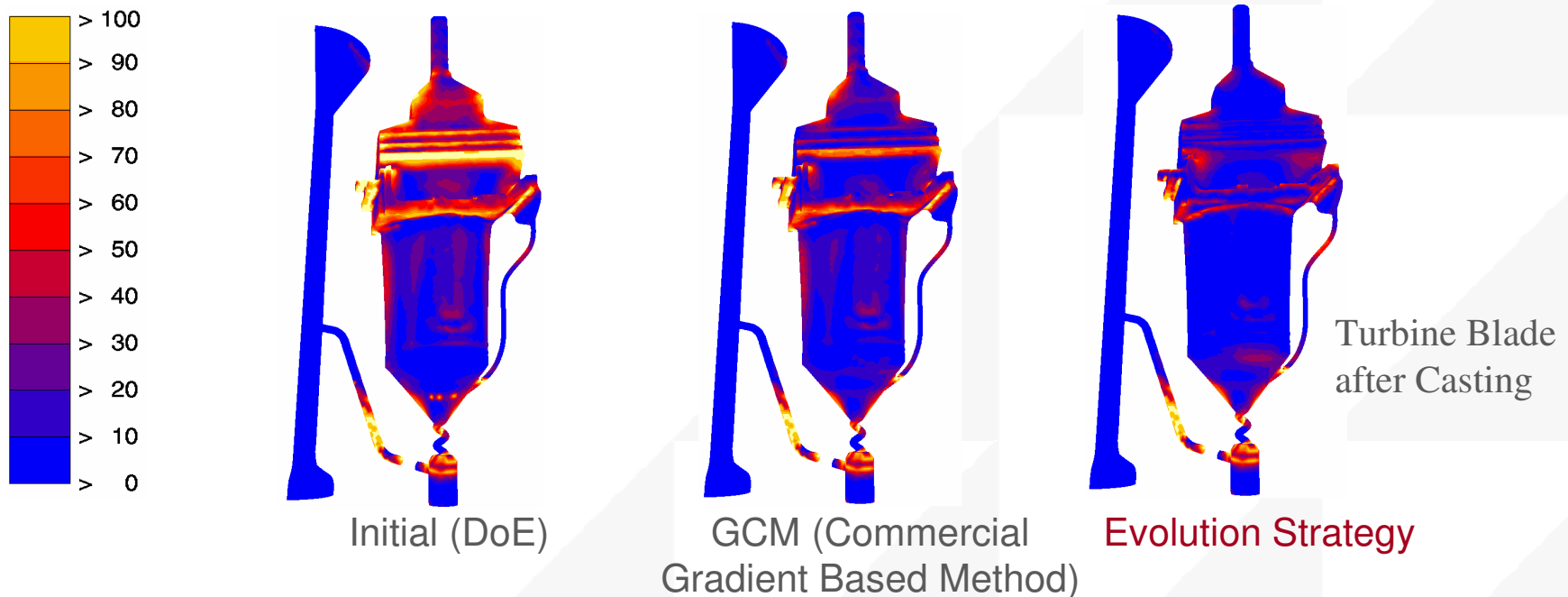


- ▲ **Objective:** Minimization of defects in the produced parts.
- ▲ **Variables:** Geometric parameters and forces.
- ▲ **ES finds very good results in short time**
- ▲ Computationally expensive simulation



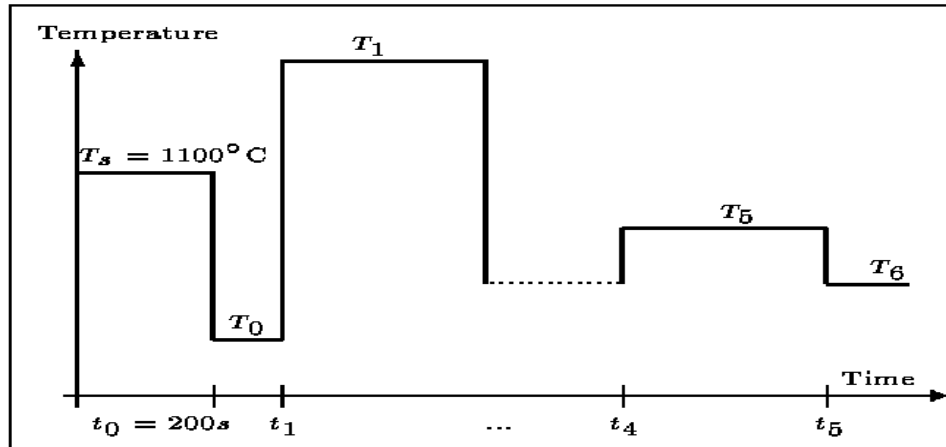
Bridgeman Casting Process

- ▲ Objective: Max. homogeneity of workpiece after Casting Process
- ▲ Variables: 18 continuous speed variables for Casting Schedule
- ▲ Computationally expensive simulation (up to 32h simulation time)

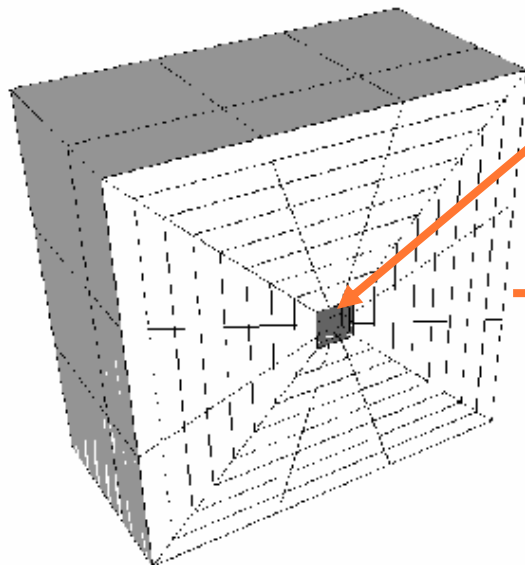


Steel Cube Temperature Control

Minimize the deviation of temperature at the cube's Surface to 1000°C !



Input: Temperature Profile (12 Variables
7 Temperatures
and 5 Time-Steps)



ΔT_{max}

Algorithm	100 OFE	200 OFE	1000 OFE
SQP	148	67.7	59
Conjugate directions	135	135	135
Pattern search	157	147	48
DSCP/Ros enbrock	88	38	29
Complex strategy	152	152	111
(1,3)-DES	91	67	67
(1,5)-DES	53	48	48
(1,7)-DES	110	58	58
(1,10)-DES	152	80	28
MAES	122	65	12

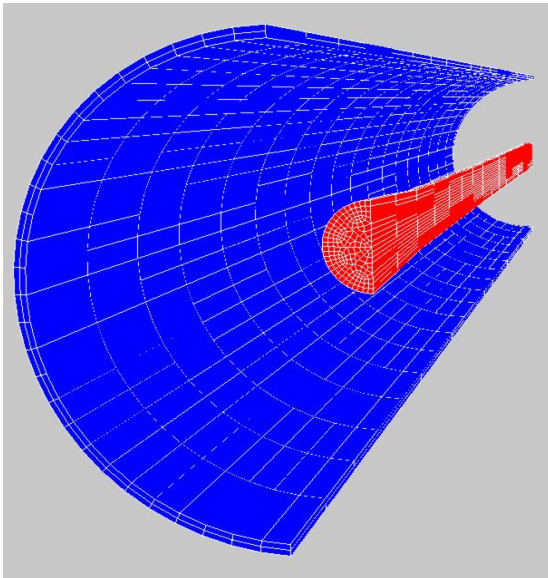
Siemens C Reactor

- Maximisation of growth speed
- Minimisation of diameter differences

FLUENT: Simulation of fluid flow
CASTS: Calculation of Temperature and concentration field

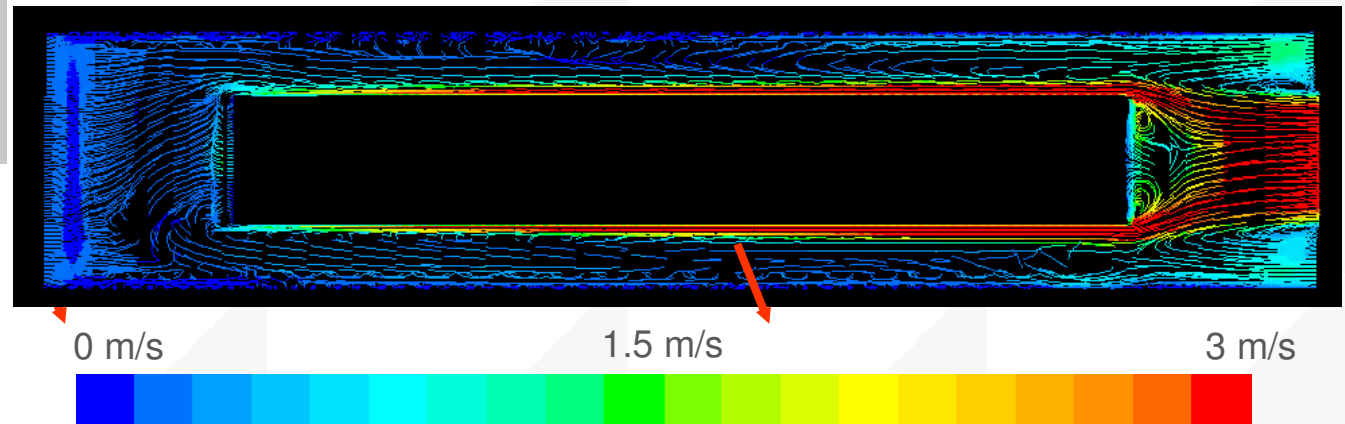
Optimisation of 15 process parameters:

Production time 35 hours → 30 hours



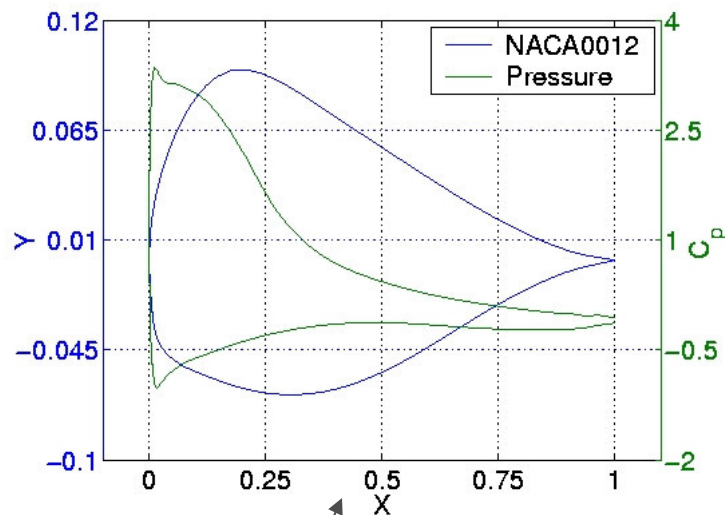
Reaction Gas TCS

Growing High Purity Silicon Rod



Multipoint Airfoil Optimiziation

- ▲ **Objective:** Find **pressure** profiles that are a **compromise** between two given **target pressure** distributions under two given flow conditions!
- ▲ **Variables:** 12 to 18 Bezier points for the airfoil



High Lift!

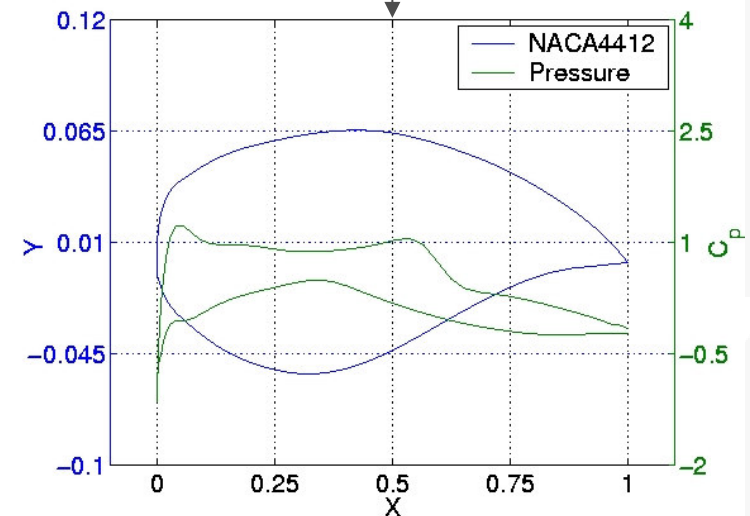


Start

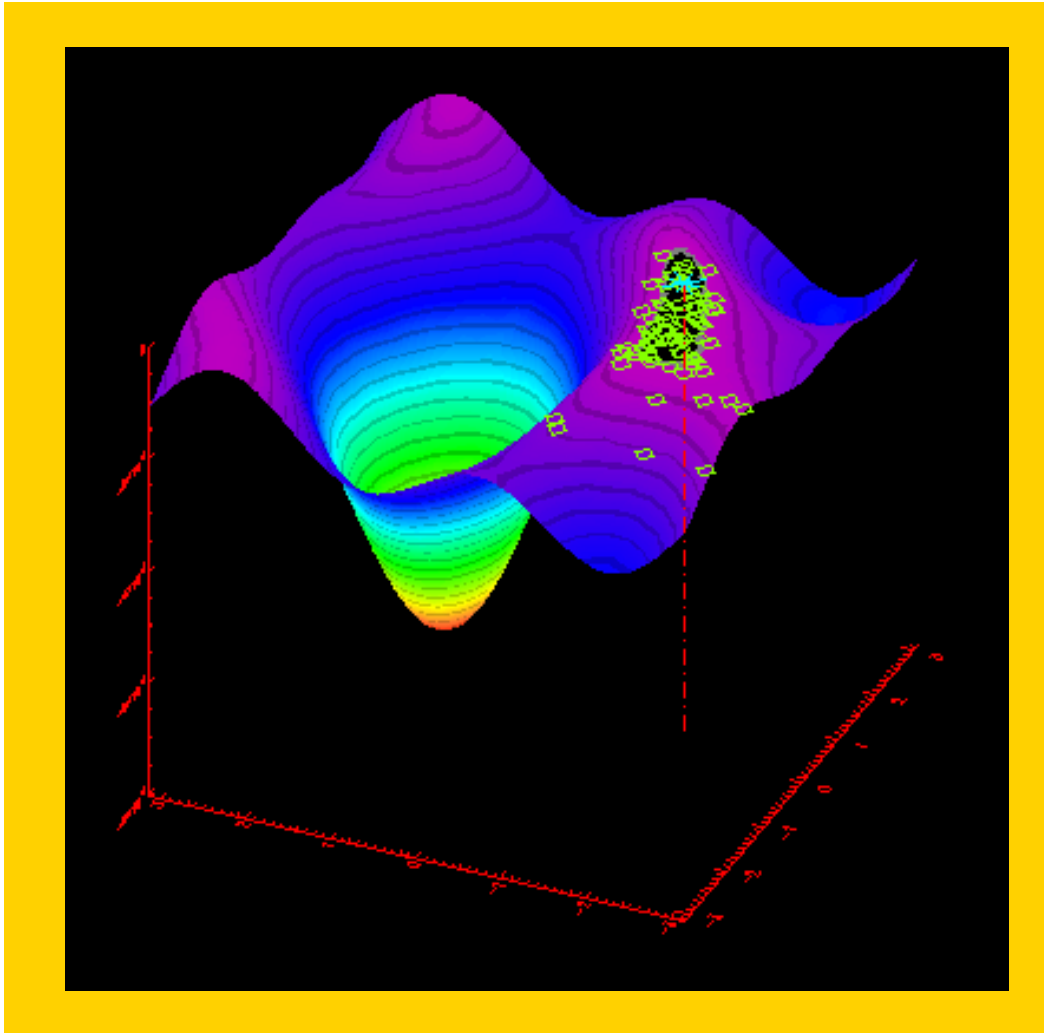


Cruise

Low Drag!

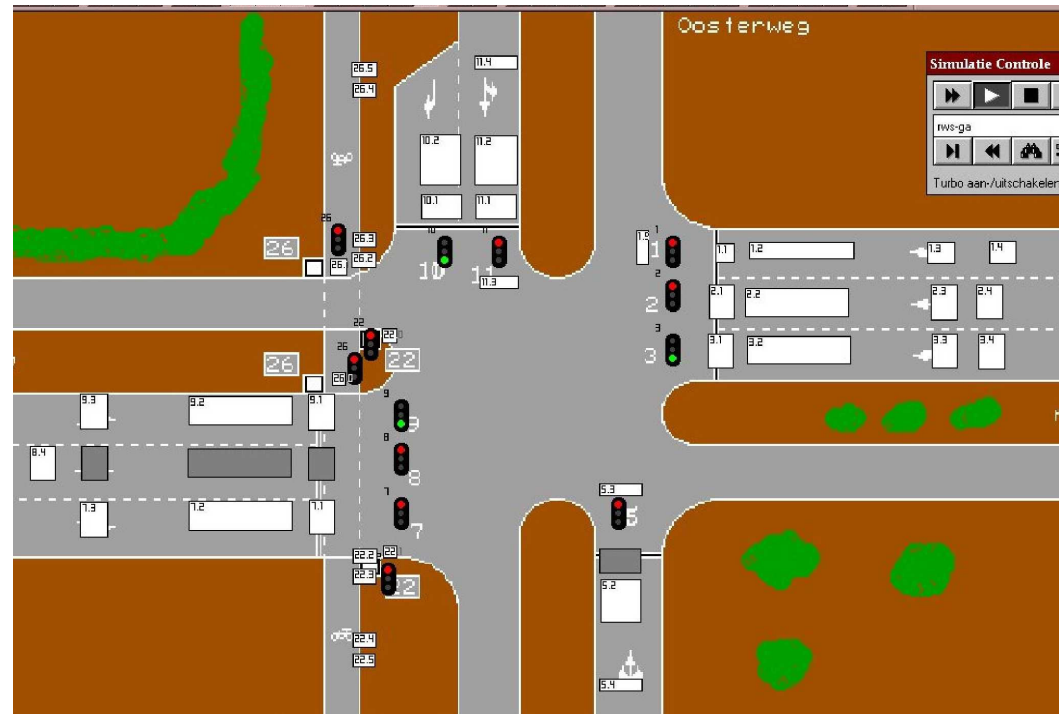


Optimum tracking of an ES



- ▲ Dynamic function
- ▲ 30-dimensional
- ▲ 3D-projection

Traffic Light Control Optimization



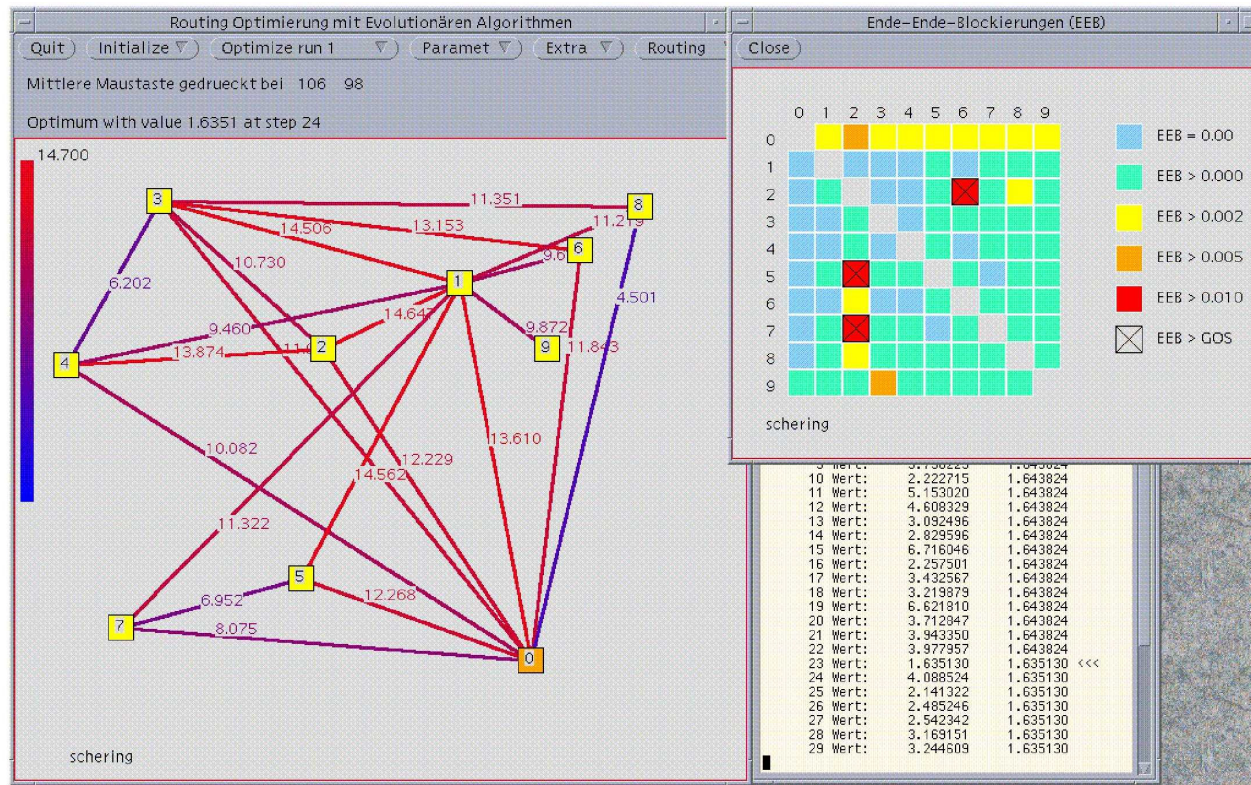
- ▲ **Objective:** Minimization of total delay / number of stops
- ▲ **Variables:** Green times for next switching schedule
- ▲ **Dynamic optimization**, depending on actual traffic
- ▲ Better results (3-5%)
- ▲ Higher flexibility than with traditional controllers

Optimization of elevator control



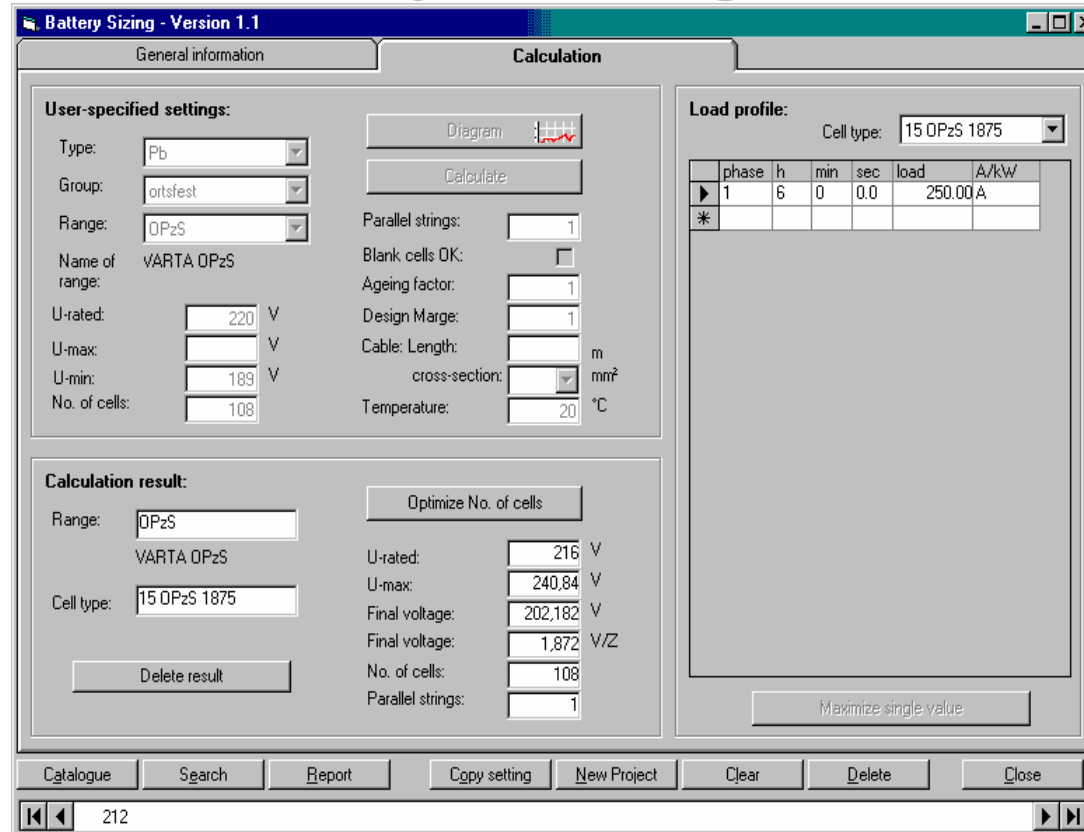
- ▲ Minimization of passenger waiting times.
- ▲ Better results (~10%) than with traditional controller.
- ▲ **Dynamic optimization**, depending on actual traffic.

Optimization of network routing



- ▲ Minimization of end-to-end-blockings under service constraints.
- ▲ Optimization of routing tables for existing, hard-wired networks.
- ▲ 10%-1000% improvement.

Automatic battery configuration



Battery Sizing - Version 1.1

Calculation

User-specified settings:

Type: Pb
Group: ortsfest
Range: OPzS
Name of range: VARTA OPzS
U-rated: 220 V
U-max: V
U-min: 189 V
No. of cells: 108

Parallel strings: 1
Blank cells OK:
Ageing factor: 1
Design Margin: 1
Cable Length: m
cross-section: mm²
Temperature: 20 °C

Calculation result:

Range: OPzS
VARTA OPzS
Cell type: 15 OPzS 1875

U-rated: 216 V
U-max: 240,84 V
Final voltage: 202,182 V
Final voltage: 1,872 V/Z
No. of cells: 108
Parallel strings: 1

Load profile:
Cell type: 15 OPzS 1875

phase	h	min	sec	load	A/kw
1	6	0	0.0	250.00	A
*					

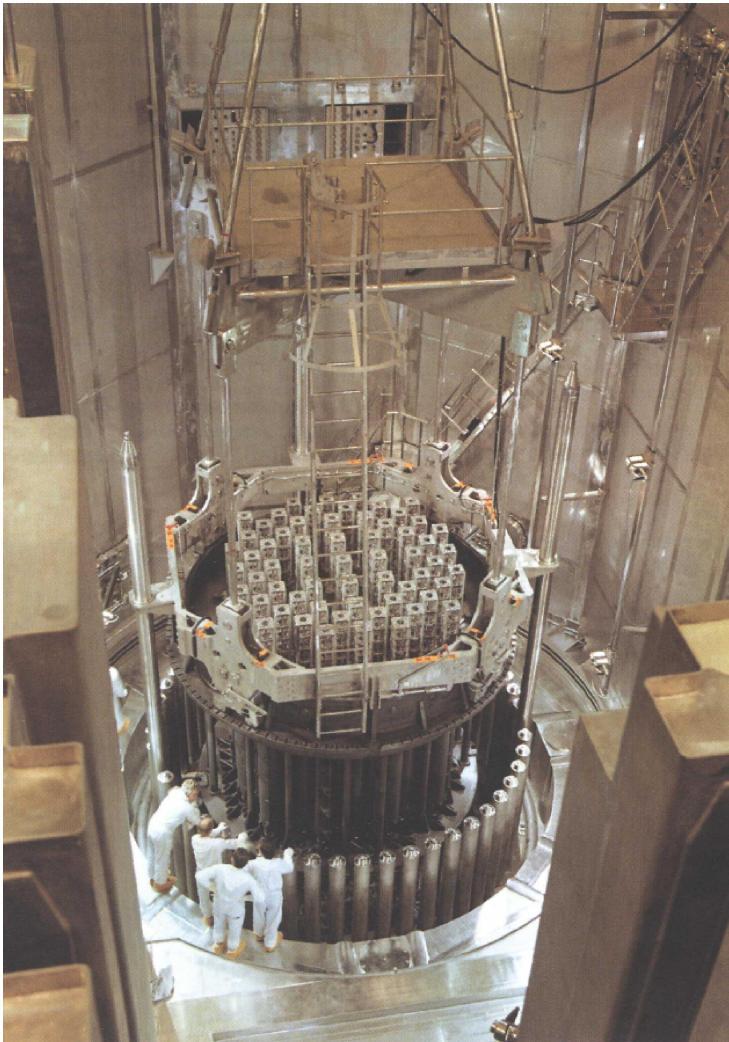
Buttons: Catalogue, Search, Report, Copy setting, New Project, Clear, Delete, Close

Page: 212

- ▲ Configuration and optimization of industry batteries.
- ▲ Based on user specifications, given to the system.
- ▲ Internet-Configurator (Baan, Hawker, NuTech).

Optimization of reactor fueling.

SIEMENS



- ▲ Minimization of total costs.
- ▲ Creates new fuel assembly reload patterns.
- ▲ **Clear improvements (1%-5%) of existing expert solutions.**
- ▲ Huge cost saving.

Final Remarks



Is it Worth Doing It ?

- ▲ Many competitors – indicates importance
- ▲ Having the best algorithm helps
- ▲ Having an easy to use algorithm is more important
- ▲ Self-adaptation is a wonderful feature
- ▲ You need to be fast & good
- ▲ Workflow integration is highest priority
- ▲ It's tough to make them pay what it is really worth !

Final Remarks

- ▲ Would not work without continuously improving ES
- ▲ Have not published results for 6 years
- ▲ If challenging problems can be handled, clients have more challenging ones
- ▲ See www.nutechsolutions.com

Partnership



ANALYSIS

SOFTWARE

ENGINEERING

.....

- ▲ Evolution Strategy Module for Optimus available.
- ▲ Distribution D, A, CH by FE Design.
- ▲ Effective as of April 2005.

Thank you for your Attention !

Questions ?

