#### **Evolutionary Design Search, Exploration and Optimisation**

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#### Setting the Scene

- 1. Design Search, Exploration and Optimisation
- 2. SEO Spectrum across Conceptual, Embodiment and Detailed Design
- 3. Design Attributes of EC
- 4. Search and Exploration during Conceptual Design

#### **Design Search**

- Search across space of design solutions
- i.e. across all possible variable combinations

• Driven by single criteria or by multiple criteria (qualitative and quantitative) which may conflict

• Relatively fixed design space - variables, constraints and objectives are pretty well defined

• Designer not necessarily interested in 'best' solution - wishes to better understand what solutions are available and their characteristics.

#### Exploration

• Search moves outside initial variable bounds, constraints soften, objective preferences change - any combination of these actions.

i.e. Introduces change to *design space and fitness landscape* 

• Design *exploration* - seeking and selecting solutions from new space evolved from initial definition.

• Primarily takes place during conceptual stages of design – leads to innovation and creativity?



• Degree / extent of exploration far greater where subjective evaluation plays a major role

e.g. product design, architectural / structural design

• Aesthetics must be taken into consideration – largely explorative, innovative and creative.

• Satisfying aesthetic considerations necessitates engineering exploration

- innovative structural developments?

- innovative considerations for services etc?

#### Why Evolutionary Computing?

Common attributes of the techniques of particular relevance to design SEO include:

- no requirement for apriori knowledge relating to problem.
- Wide range of model type eg. discrete, continuous, mixed-integer, quantitative, qualitative, etc. can be utilised.
- excellent exploratory capabilities diverse sampling of design space continues throughout search process

• ability to avoid local optima - continuing random sampling prevents premature convergence.

• ability to handle high dimensionality.

• robustness across wide range of problem class can outperform deterministic optimisation algorithms across wider range of problem classes where high modality, high dimension, conflicting criteria and heavy constraint are in evidence.

• provision of multiple good solutions - can identify multiple high-performance solutions

• multi-objective approaches easily and successfully integrated with various EC techniques;

• can locate region of global optimum - extensive local search may be required to isolate the optimum. Introduction of deterministic gradient-based optimisers or local search techniques can be of considerable utility.

• can be utilised in an interactive search and exploration manner to capture user experiential knowledge and intuition

Agent-based technologies can be easily integrated to further support search and exploration, knowledge extraction and visualisation.

Although all techniques offer utility individually appropriate combinations of them can provide very powerful complementary global and local design search, exploration and optimisation capabilities

#### **Evolutionary Search and Exploration during Conceptual Design**

• Tutorial concentrates upon integration during early stages of design

• Early stages characterised by poor definition, uncertainty, multiple qualitative and quantitative objectives, problem reformulation and moving goalposts.

• High degree of user involvement - varying degrees of subjective solution evaluation.

•Evolutionary systems required that can capture designer experiential knowledge and intuition

Primary area of my research since late 1980's with projects relating to:

• Design of novel pneumatic hydropower systems;

• Cluster-oriented GAs - integration with gas turbine design, preliminary air-frame design, drug design and discovery, ROV design;

• Whole system design - structured GA representations for exploration of discrete/ continuous problem spaces;

• Various hybrid techniques for constraint satisfaction in aerospace and power engineering domains;

• Use of GP for systems identification – evolution of approximate design representations to aid search and exploration;

Further details of all these projects in Evolutionary and Adaptive Computing in Engineering Design. Parmee I. C., Springer Verlag, 2001.

#### More recent work concentrates upon development of interactive evolutionary design systems (IEDS) involving:

• Cluster-oriented GAs for high-performance solution generation and extraction (both single and multi-objective)

- Co-evolutionary multi-objective satisfaction;
- Fuzzy preferences techniques for objective / constraint ranking;
- Software agent-based systems for data processing and visualisation and objective / constraint negotiation.

# What is Interactive or User-centric Evolutionary Design?

• Generally relates to partial or complete human evaluation of fitness of solutions generated from evolutionary search.

• Quantitative evaluation difficult if not impossible to achieve. Examples of application:

Graphic arts and animation (Sims K ,1991); Automotive design (Graf J., Banzhaf W.,1995); Food engineering (Herdy M., 1997.)

Database retrieval (Shiraki H., Saito H., 1996.)

All rely upon a human-centred, subjective evaluation of the fitness of a particular design, image, taste etc

Partial human evaluation also in evidence, e.g.

• User interaction relating to an evolutionary nurse scheduling system - schedule model provides quantitative evaluation but model not adequate in terms of changing requirements, qualitative aspects etc. User must add new constraints to generate satisfactory solutions (Inoue T., 1999).

• Design of biomolecular systems enhanced by partial interactive evolution. Optimal bio-molecule combinations improved by user-introduction of new combinations into selected genetic algorithm generations (Levine D. 1997).

# Recent examples of IEC/UcEC in engineering domains:

• Carnahan and Dorris's work [2003] graphical design of industrial warning sign icons.

• Development of hearing-aid signal processing capabilities - user's evaluation of hearing utilised during fitting process [Takagi et al, 1999].

• Caleb-Solly and Smith (2002) – identification of regions of interest in images during hot rolled steel surface inspection – supports defect recognition.

• Parmee (2001) - provides information to user which supports better understanding of design domain and iterative improvement in problem representation

# Complete human evaluation could be viewed as **explicit** interaction

Partial evaluation could be considered **less explicit** interaction

#### Implicit interaction? -

Recent work: on-line assessment of student navigation of web-based tutorial systems [Semet et al 2003] - data then utilised to optimize web layout to facilitate future student usage -

Users unaware of their role in the evolution of the system.

# Spectrum of IEC approaches based upon explicit /implicit nature [Parmee 2003] :

mplicit 🔸 🗕			<ul> <li>Explicit</li> </ul>	
Process Evaluation	Problem Definition	Subjective Evaluation	Subjective Selection	
<b></b>	I	1		
User unaware of evaluation of their actions. Machine-based monitoring of user choices and evolution of optimal paths / optimal paths / optimas e.g. Semet's web based tutorials.	Continuous interaction Monitoring of solutions, objectives constraints and problem structure. Problem structure. Problem structure. ation; knowledge capture; evolution of problem space e.g. Parmee's interactive evolutionary design	Partial User Solution Evaluation Machine-based evaluation plus user evaluation, Solution injection, modification, transformation e.g. Levine's biotechnology application; Innoue's nurse scheduling system	100% User Solution Evaluation Art, Graphics, Music etc e.g. Sim's evolutionary art; Unemi's evolutionary graphics; Carnahan's hazard icons.	

Let's explore evolutionary conceptual design approaches that lie along this explicit / implicit interaction spectrum commencing at the more explicit end and progressing through partial interaction to more implicit interaction.

Should illustrate many of the considerations to take into account when integrating EC wth conceptual design.

#### The Design Representation Problem

How do we best represent complex structures within evolutionary SEO design systems such that:

- ✓ The search is efficient
- ✓ Possible design solutions are not compromised

✓ Restrictions of 'traditional' representations such as binary, real number and tree based are overcome?

Many representations possible each offering utility during various stages of design e.g

- Fuzzy rule-based models;
- Statistical response surfaces;
- Neural net / RBF representations;
- Cellular Automata representations;
- Multi-agent based simulations;
- Object-oriented / component-based representations;
- Mathematical models.

#### Example:

A component-based representation adopted in recent work relating to the **Integration of Aesthetic Criteria with User-centric Evolutionary Design** of bridges and 'urban furniture' (Machwe & Parmee 2005).

Structures are developed from range of simple primitive shapes. This allows required flexibility.

- **Construction and Repair Agents (CARAs)** assemble primitives in accordance with appropriate rule-sets.
- **CARAs** create initial population then EP system performs SEO within the space of possible structures.
- Disruptive mutation operatorions monitored by **CARAs** repair carried out if necessary.





The Construction and Repair Agent (C.A.R.A.)

- Major problem with component based representation: *how to bring all components together in a sensible manner for initial population?*
- Solution: Have a rule-based construction agent build the initial population within overall user constraints (e.g. span length/maximum height).



# EVOLUTIONARY SEARCH AND EXPLORATION Evolutionary Programming (EP) utilised to avoid problems relating to unrestricted crossover. Rule based mutation. Tournament selection.

#### **Mutation Operation**

- Rule based mutation.
- Rules used for mutation depend on the type of element selected for mutation.
- Supports can only change thickness and location. Height remains constant.
- Span elements can only change thickness.





Aesthetics take into account both rule subjective factors.	-based and
In present system following aesthetics coded:	have been
Symmetry of support placement	(A1)
Slenderness Ratio	(A2)
Uniformity in thickness of supports	(A3)
Uniformity in thickness of span sectio	ns (A4)
Fach defined aesthetic is evaluated by	a separate
Each defined aesthetic is evaluated by	a separate

In addition, **'User assigned fitness' (Ufit)** is fitness given to design by user on a scale of 0 to 10 (10 being the best).

User can also mark solutions for preservation into the next generation.

User stipulates the frequency of user interaction (e.g. once every 10 generations).



Aesthetically pleasing shapes after 30 generations with user evaluation at every tenth generation.

Coded aesthetic criteria (A1 to A4) clearly reflected. Span elements are same size. Supports are of nearly uniform thickness and their placement is also symmetric.



#### Machine-learning and Reducing User-fatigue

Machine-learning techniques now introduced to reduce degree of user-evaluation thereby reducing fatigue

Objective is on-line learning of user aesthetic preference -

Machine-based judgement slowly replaces human judgement as generations progress.

A Case-based reasoning approach has proved best way forward.

(see Machwe & Parmee; Design 2006, Dubrovnic)

#### Free-form Design of Urban Seating Arrangements

'Urban furniture' work far less constrained with more complex CARA agent rules

Commenced with bench-like structiures and have progressed to much less restricted form comprising multiple components

Still a mixture of machine-based and human-based evaluation.

Examples follow.





#### Significant utility to engineering/product/industrial designer across this spectrum in terms of direct utilization of IEC and in the integration of various IEC elements within suites of computer-aided design tools.

In this second instance, we will concentrate upon interactive / user-centric aspects relating to:

- evolutionary design search and exploration;
- high-quality information generation;
- knowledge discovery;
- knowledge capture and integration;
- design space evolution.

This lies further towards the implicit end of the spectrum

#### Interactive Evolutionary Design Systems

 Major potential - utilisation of EC algorithms as gatherers of optimal / high-quality design information

• Info can be collated and integrated with humanbased decision-making processes.

• Approach can capture designer experiential knowledge and intuition within further evolutionary search

• Supports exploration outside of initial constraint, objective and variable parameter bounds

- Off-line analysis of search data supports iterative designer/machine-based refinement of design space [Parmee, I.C., 1996].
- Immersive system? designer part of iterative loop
- Multi-disciplinary aspects considered at early stage
- Global considerations represented simply as objectives with associated preferences
- Effect upon emerging solutions identified during iterative development of design space.



#### **Initial IEDS Components**

#### Information extraction:

COGAs rapidly identify high performance (HP) design regions relating to single or multiple objectives.

Good solution set cover of identified regions supports extraction of relevant design information

Information mined, processed and presented to the designer in succinct graphics .

Info relates to: Solution robustness, revision of variable ranges, conversion from variable to fixed parameters, degree of objective conflict, sensitivity of objectives to each variable

Solutions describing HP regions can be projected onto any 2D variable hyperplane:





	Much More Important than	©I	
	More Important than	c	
Takeoff Distance	Less Important than	o	Ferry Range
	Much Less Important than	•	
			Confirm

#### iii) Co-evolutionary Multi-objective convergence:

Co-evolutionary MO strategy developed where each evolutionary process attempts to converge upon a particular objective [Parmee I., Watson A., 1999]

Penalty functions penalize best solutions in each process relative to Euclidean distance i.e. HP solutions far apart design space have their fitness reduced.

Results in all processes converging upon best compromise regions in the design space i.e. regions containing best solutions for all objectives.





Graphical visualization of each process tracking across approximate Pareto surface is generated

Direct mapping between solutions on the Pareto surface and their location in variable space readily available.

Integration of Preference component allows designer to interact with the system and to converge upon differing regions of Pareto surface



#### iv) Software Agents:

Software agents monitor co-evolutionary processes

Recognise states relating to degree of convergence, constraint satisfaction and multi-objective satisfaction

Negotiating agent systems utilising Preference module have been established

Identify solutions satisfying range of design scenarios re multiple objectives and ideal variable values [Cvetcovic D., Parmee I. C., 2002].

#### Where do we go from here?

# Can we develop user-centred intelligent systems that during conceptual design:

Support exploration of multi-variate problem space?

Provide succinct graphical representation of complex relationships from various perspectives?

Support a better (intuitional?) understanding of complex relationships?

#### **Cognitive Aspects**

Can we position these approaches in terms of cognitive science?

Regular achievement of HP solutions to complex problems through manipulation of multiple input variables becomes easier as familiarity with problem increases [Berry D. C., Broadbent D. E., 1984].

Learning process is implicit as subjects have great difficulty in describing how they achieved such results.

Other research shows that repeated patterns in data sets that support success in certain tasks can be recognized [Lewicki P., Hill T., Czyzewska M., 1992].

Subsequent investigation revealed that patterns could not be consciously detected by the subjects even when given opportunity to extensively study the data. • Westcotts's 'successful intuitives' and 'cautious successes' - sub-groups who require differing amounts of information to solve complex problems.

• Former group comfortable exploring uncertainty - confident in arriving at correct solutions based upon small amounts of information

• Latter group prefer structure, certainty, control and far more information to arrive at successful conclusion.

CAD caters for latter group rather than former. Sufficient data only available during later stages of design - satisfies CAD tools and 'cautious successes'.

Early design and 'successful intuitives' poorly supported

Need to redress this imbalance.

#### A Step Further: Data Mining COGA Output

Recent research further concentrating upon info generation / extraction

Focuses upon variable / objective space interaction

How can we support designer when concurrently negotiating these two *n*-dimensional spaces?

Current COGA utilisation in combinatorial drug design and in early design of underwater vehicles.

Results shown based upon previous IEDS design domain:

#### Preliminary military airframe - BAE Systems

- Characterised by uncertain requirements and fuzzy objectives
- Long gestation periods between initial design brief and realisation of product.
- Changes in operational requirements + technological advances
- Demand for responsive, highly flexible strategy design change / compromise inherent features.

1. Climb Mach	4. Gross Wing	7. Wing Lead
Number	Plan Area (GWP)	Edge Sweep
(CLMIN)		(WLES)
2. Cruise	5. Wing Aspect	8. Wing T/C
Height (CH)	Ratio (WAR)	Ratio (WTCR)
3. Cruise	6. Wing Taper	9. By Pass
Mach Number	Ratio (WTR)	Ratio (BPR)
(CRMN)		
Mi	niCAPS Input Varia	ibles

#### **Cluster-oriented Genetic Algorithms**

COGAs identify high performance regions of complex preliminary / conceptual design spaces

Approach can be utilised to generate highly relevant design information relating to single, multi-objective and constrained problem domains

#### How do COGAs operate?

- Highly explorative GA / GAs
- Solutions extracted and passed through Adaptive Filter

• Better solutions pass into Final Clustering Set - defines HP regions

[Parmee, I.C., 1996, Parmee I. C., Bonham C. R., 2000, Bonham C. R., Parmee I. C., 1999a, Bonham C. R., Parmee I. C., 1999b]





Parallel Co-ordinate plots [Inselberg, A., 1985] show each variable dimension vertically parallel to each other. Points corresponding to solution's variable values can be plotted on each vertical variable axis.

Distribution of ATR1 HP region solutions across all variable dimensions

Distribution of solutions in all variable dimensions and correlation between dimensions can be shown

Information too dense when dealing with multiobjectives

Combination of Box Plot representation and Parallel Co-ordinates relating to all objectives contains several layers of design information

Developed Parallel Co-ordinate Box Plot -PCBP [Parmee and Johnson, 2004] provides all information in single graphic





Variable attribute relevance plus standard skewness analysis of [Han, J., Kamber, M., 2001] COGA-generated HP solutions verifies visual information available in the Parallel Co-ordinate Box Plot.

Information gain ranking identifies variables 4, 5, 7 and 8 as those variables to which the objective set is most sensitive

Skewness analysis also confirms visual information available in the plot. Further details of this work can be found in [Johnson and Parmee, 2004].

Input Variable	Skewness		Correlation Coefficient		Inform- ation Gain	Rank		
	ATR1	FR	SEP1	ATR1	FR	SEP1	ATR1, FR& SEP1	1
1. CLMN	-0.481	-0.888	0.013	0.095	0.136	-0.086	0.026	7
2. CH	-0.566	-0.193	-0.430	0.059	0.307	0.043	0.068	6
3. CMN	-0.475	-1.123	-0.151	0.051	0.181	0.049	0.118	5
4. GWPA	-1.653	-1.758	1.280	0.170	0.463	-0.566	0.953	1
5. WAR	0.501	-0.404	0.761	-0.257	0.251	-0.207	0.255	4
6. WTR	-0.230	0.172	-0.008	0.013	0.001	-0.018	0.013	9
7. WLES	-1.351	1.098	0.315	0.478	-0.349	-0.071	0.265	3
8. WTCR	1.059	-0.922	1.073	-0.55	0.249	-0.521	0.419	2
9. BPR	-0.460	-0.757	-0.127	0.141	0.119	0.019	0.014	8
9. BPR	-0.460	-0.757 Mean of Ir	-0.127 formatic	0.141 on Gain	0.119	0.019	0.014	8



iv) View related variable hyperplane projections for a different perspective of spatial distribution of objectives' high-performance regions

Access to such hyperplanes driven by simple clicking operations on selected variable axes

v) View projections of high-performance regions on objective space – direct mapping between variable and objective space









COGAs can provide much high-quality information relating to solution distribution in both variable and objective space

• A direct mapping can be achieved between these two spaces

• Good approximations to relevant Pareto fronts can be identified.

#### Current Research - Agent-based Activities

Established data mining and statistical analysis tools drive agent-based activity

Support degree of autonomous action which supplements designer interaction with system.

e.g. data processing, designer interrogation and / or the provision of textual advice

Agency should reduce amount of information and cognitive load, allowing greater concentration upon primary design characteristics.

Agency mustn't reduce designer interaction with the system to the extent that 'hands on' and implicit learning aspects are diminished.

Agency should enhance rather than replace understanding by improving clarity through provision of differing perspectives relating to complex dependencies whilst minimising mundane tasks

#### **Questions posed:**

Can unconscious recognition of variable, constraint and objective relationships play a role in design problem-solving processes?

Supports overall capability to unconsciously handle far more dimensions of information whilst consciously manipulating and attempting to understand those of prime importance at any particular moment? Computer-aided conceptual design systems that support implicit learning could represent a new approach.

Possibly best way forward?

## THANKYOU!

.....but before we end.....

**Discovery in Design: Peoplecentred Computational Issues** 

Initially an AHRB / EPSRC 'Designing for the 21<sup>st</sup> Century' Cluster

Now the 'Institute for Peoplecentred Computation http://www.ip-cc.org.uk

#### **Cluster and Institute Objectives:**

'.....to identify primary research aspects concerning the development of people-centred computational conceptual design environments that engender concept and knowledge discovery across diverse design domains'.

## Why?

Early design characterised by:

• human-centric concept formulation and development ;

• uncertainty due to lack of data / information / knowledge and poor problem definition;

• correspondingly low-fidelity computational representation (if any, initially);

Design activity extends across multiple domains and disciplines.

Current CAD tools characterised by:

low-level, inflexible designer interaction;

• requirement for relatively high product definition;

• high-fidelity computational representation;

CAD is domain-specific (mainly engineering). Little or no exploitation of cross-domain experience.

#### This imbalance must be addressed

Current massive computational capability largely unavailable to conceptual design processes

Major savings possible in design lead-time;

During early design, Innovation + Creativity = More Competitive Products

#### How?

# Via investigation of **people-centred issues** relating to (for instance):

- concept representation and simulation;
- design space search and exploration;
- data mining and processing;
- computationally intelligent systems;
- machine-based enabling and bridging technologies;
- information visualization and presentation.

#### ....and human-computer interaction and cognitive aspects such as:

- assimilation of information relating to multivariate and multi-criteria relationships;
- knowledge extraction and knowledge capture;
- subjective solution evaluation;
- implicit learning and tacit knowledge.

## Who do we have?

Researchers and Practitioners from:

- Engineering: Aerospace, Civil,
- Mechanical, Telecoms, Marine etc
- Computing: Software Engineering, Networks, e-Science.
- Biotechnology: Compound, Drug, Biosensor, Material design.
- Psychology: Human-computer Interaction, etc
- Media: Visual and Virtual Product design.

## Who else do we need?

- Organisational and Business design??
- Financial System and Product design??
- Hardware / Electronic design??
- Chemical Plant / Process design??

Others (suggestions welcome)??

# What People-centred issues are we investigating?

Amongst other, emerging issues, the manner in which:

• collation / analysis of information aids understanding and reduces uncertainty;

• iterative human / machine based evaluation increases confidence and fosters a better understanding of inherent complexities; • knowledge acquisition leads to problem reformulation through discovery and gradual evolution of concepts / design representation;

• improved understanding promotes radical design change.

## How can Computational Intelligence contribute?

• Exploration of multi-variate spaces described by some design model generally essential;

- Search, exploration and problem
- representation therefore key elements;

• Utility of relatively established technologies will be reassessed in the light of their current usage.

#### For example:

- Rule-based representation via multi-agent simulations, fuzzy inference models.
- Data-based models / response curves generated from statistical or neural network techniques.
- Evolutionary search and exploration processes to negotiate resulting complex design spaces.
- Multi-agent systems to support associated data processing and presentation.
- On-line machine-learning techniques to enable degree of autonomous software agent activity.

#### We need to extend investigations into:

- associated areas of research;
- the potential of new, emerging technologies;
- future of human-centred intelligent systems based upon identified conceptual design requirements.

## **Enabling Computing Technologies**

CI techniques not stand-alone - need investigation alongside range of enabling technologies . For instance:

- Data mining and processing;
- Visualisation techniques understanding highdimensional data relationships
- High performance computing rapid response to design change.
- In-house and global grid-based supporting systems.

#### Things to consider......

- Whilst focussing upon primary research issues we must maintain diversity in our approach;
- When focussing upon a specific technology we must assess it across many disciplines;
- When focussing on a particular discipline we should constantly cross-reference across other domains.
- Special interest groups should comprise multiple disciplines.

#### • If a computational technology does not appear to offer utility in a particular discipline then we should figure out why and attempt to identify modifications to that technology or a new paradigm that can offer utility

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